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CALCULATING COMPRESSIBLE LAMINAR AND TURBULENT BOUNDARY LAYERS IN ARBITRARY PRESSURE GRADIENTS FORTRAN PROGRAM FOR

by William D. McNally

Lewis Research Center Cleveland, Obio 44135

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FORTRAN PROGRAM FOR CALCULATING COMPRESSIBLE LAMINAR

AND TURBULENT BOUNDARY LAYERS IN ARBITRARY

PRESSURE GRADIENTS

by William D. McNally

Lewis Research Center

SUMMARY

"integral" methods. In the laminar regime, a single ordinary differential equation, the order ordinary differential equations, the momentum and moment-of-momentum integral gradient. Cohen and Reshotko's method is used for the calculation of the laminar boundmomentum integral equation, is solved numerically. For turbulent flow, coupled firstcompressible laminar and turbulent boundary-layer equations in an arbitrary pressure computer program was written which gives the solution of the two-dimensional, ary layer, and Sasman and Cresci's method for the turbulent boundary layer. equations, are solved using Runge-Kutta techniques.

Ulrich-Granville method; or the user may specify a transition point, thus forcing transi-Transition from laminar to turbulent boundary layer is predicted by the Schlichtingtion. Separation is predicted in the laminar regime when negative skin friction occurs. Separation is predicted for turbulent flow when the level of incompressible form factor reaches a specified limit.

The program allows a variety of initial conditions: laminar boundary layer at a stagwith initial displacement or momentum thickness given, or turbulent boundary layer with nation point, laminar boundary layer on a sharp leading edge, laminar boundary layer initial displacement and momentum thicknesses given.

cipal boundary-layer parameters, such as displacement thickness, momentum thickness, The program input consists of surface geometry, a pressure or velocity distribution external to the boundary layer, wall temperatures, total flow conditions, and initial values of displacement and momentum thickness, if any. The output includes all the prinform factor, skin friction, heat transfer, and velocity profiles.

This report includes a listing of the FORTRAN IV computer program with an explanaical examples are included to illustrate the input and show what type of results are obtion of the equations involved, the solution methods, and the preparation of input. tained. Running times are less than 1 minute on IBM-7094 equipment.

INTRODUCTION

allows the inclusion of real flow effects into flow models used in the analytical prediction turbomachinery is one such problem area, since boundary layers influence the performmand an understanding of the growth and properties of boundary layers. Flow through There are many analysis and design problems in the field of aeronautics which deance and losses of turbomachines to a great degree. A computer program which predicts the development of boundary layers under known conditions of pressure gradient of flow and performance in turbomachines.

ideal blade-surface velocity distributions, which can then be used to make an analysis of Known conditions of pressure gradient can be obtained either analytically or experion the blade-to-blade surface of revolution of turbomachines. These programs compute Programs already exist (refs. 1 to 3) for the analytical solution of ideal flow boundary-layer development. Experimental distributions of velocity or pressure may also serve as input to a boundary-layer analysis. mentally.

This report discusses a FORTRAN IV program for computing two-dimensional comsition from laminar to turbulent flow is also predicted. Two of the most applicable integral methods available have been used in the laminar and turbulent sections of the propressible laminar and turbulent boundary layers in arbitrary pressure gradients.

Sasman and Cresci's method (ref. 5) It is an approximate method of integral type for compressible laminar cases Cohen and Reshotko's method (ref. 4) is used for the solution of the laminar boundmethod, and involves coupled momentum and moment-of-momentum differential equais used in the turbulent-boundary-layer section of the program. It is also an integral tions. It is an extension of Reshotko and Tucker's method (ref. 6) for compressible boundary layer with heat transfer and arbitrary gradients. The Schlichting-Ulrich-Granville method (refs. 7 to 9) is used in the program for predicting transition. with heat transfer and arbitrary surface gradients. ary layer.

The program allows the arbitrary selection of initial values in both laminar and turdimensional case with subsonic or supersonic Mach numbers. It is not restricted to the also allows reattachment after laminar separation. The program will handle any twobulent regions, as well as the selection of the point of transition if the user wishes. compressor and turbine problems which motivated its existence.

given of the input required and the output received. Numerical examples are included This report includes the FORTRAN IV computer program called BLAYER, with an A detailed explanation to illustrate the input and show what type of results are obtained. explanation of the equations involved and the method of solution.

The report is divided into two main parts: INFORMATION FOR GENERAL USER Those wishing to use the program in its and INFORMATION FOR PROGRAMMER.

Information of interest to someone who may wish to change the program is concomplete program listing, as well as descriptions of the individual subroutines and varcontains descriptions of the general method, the preparation of input, and the output re-This part contains present form need only read the first part, INFORMATION FOR GENERAL USER. tained in the second part, INFORMATION FOR PROGRAMMER.

BLAYER source deck on tape is available from COSMIC (Computer Software Management and Information Center), Computer Center, University of Georgia, Athens, 30601. The COSMIC program number is LEW-11097.

INFORMATION FOR GENERAL USER

DESCRIPTION OF METHOD

The following sections outline the basic characteristics and limitations of this program and give short descriptions of input and output characteristics. This information tailed information about program procedure and operation is contained in the sections should enable the reader to decide if the program is applicable to his needs. describing the individual subroutines.

Basic Characteristics of Program

The following statements give a general description of the characteristics of the overall program:

- (1) The program is for two-dimensional, compressible or incompressible, laminar and/or turbulent boundary layers.
- equations, the momentum and moment-of-momentum integral boundary layer equations, Ordinary differential (2) It uses integral methods rather than differential methods. are solved numerically.
- (3) The program is applicable to all types of pressure gradients favorable, zero,
- (4) Both subsonic and supersonic flows may be handled.
- fer, Prandtl number, or type of free-stream velocity distribution which many of the other cause it does not have the restrictions on compressibility, pressure gradient, heat transtrary pressure gradient and heat transfer. Cohen and Reshotko's method was chosen be-(5) The Cohen-Reshotko method (ref. 4) is used to solve the laminar boundary layer. It involves the momentum integral equation for compressible laminar cases with arbi-

It is one of the most accurate, programmable, general methods available for the laminar case. laminar methods have.

- (6) The Sasman-Cresi method (ref. 5) is used for the solution of the turbulent bound-It extends Reshotko and Tucker's analysis (ref. 6) by using more recent empirical data It involves momentum and moment-of-momentum integral boundary-layer equations for compressible turbulent cases with arbitrary gradients and heat transfer to avoid some of the problems with strong adverse pressure gradients.
- the point of transition. Both analyses are for incompressible flow, but can be applied to Granville (ref. 9) is then used to predict the distance between the point of instability and tion from laminar to turbulent boundary layer. The stability analysis of Schlichting and (7) The Schlichting-Ulrich-Granville method (refs. 7 to 9) is used to predict transi-Ulrich (refs. 7 and 8) on Pohlhausen velocity profiles leads to a method for predicting The experimental curve of compressible flow through the use of suitable transformations. where the laminar boundary layer becomes unstable.
- Schlichting-Granville criteria, (b) at a point specified by the user, or (c) through laminar (8) Transition may be accomplished in one of three ways: (a) naturally, using the separation and reattachment.
 - Separation is predicted in the turbulent regime when the level of incompressible form (9) Separation is predicted for laminar flow when negative skin friction occurs. factor passes a specified limit.
 - (10) Typical program runs on IBM-7094 equipment take less than 1/2 minute.
- (11) The program is written in FORTRAN IV, and is available from COSMIC (see INTRODUCTION).

Input and Output Characteristics

The following statements briefly describe some of the input and output features of the

- upstream Mach number, initial values (if any), and some integer constants are required. of surface points, a surface flow distribution at the X-Y points, and wall temperature at relative free-stream velocity, relative free-stream Mach number, ratio of static presthe X-Y points. Besides these four basic arrays, gas constants, stagnation conditions, (1) Input to the program consists principally of four arrays: X- and Y-coordinates Surface flow distribution can be given as any one of five quantities: static pressure, sure to total pressure, or ratio of relative velocity to critical velocity.
- pletely suppressed if initial values are given for the turbulent layer at the initial calcula-(2) Initial values may be given for displacement and momentum thicknesses in either the laminar or turbulent regions of flow, or in both. The laminar region can be comtion station.

- (3) Surface distributions of velocity may be smoothed by the program prior to the computation of surface gradients.
- metric units (Newtons, kilograms, meters, degrees Kelvin, and Joules) may be used for (4) English units (pounds force, slugs, feet, degrees Rankine, and foot-pounds) or input and output.
- displacement thickness, momentum thickness, form factor, skin friction, heat transfer, (5) Output from the program includes all the principal boundary-layer parameters: etc. Velocity profiles are calculated by using Pohlhausen's expression in the laminar regime, and the power law in the turbulent regime.

Limitations of Program

The following are the principal limitations of the program:

- (1) Surface curvature, surface roughness, initial turbulence level of the flow, and shock - boundary-layer interactions are not taken into account by the program.
- changing from point to point, such as a turbomachine rotor with change in radius along (2) The program cannot be used along surfaces where relative total pressure is However, the program could be easily extended to handle this case. streamlines.
- could also be altered for use with liquids; but alterations would be so numerous that it is (3) The program presented herein is valid only for air. However, it can be easily altered for use with other gases. These alterations are described in appendix C. suggested a separate program be written for this case.
 - (4) In strong favorable gradients, the laminar solution procedure has to be extrapostrong adverse gradients, such as those coming off the velocity peak at the leading edge of a turbomachine blade, can also give erroneous results in both the laminar and turbulent regimes. Such a condition is indicated by separation after only three or four data Very lated, so that results are questionable under these circumstances (see ref. 4).
- (5) The program does not continue computing past a point of separation, unless the user requests reattachment after the laminar separation.

BASIC EQUATIONS

turbulent sections of the program. The methods used in predicting transition and sepa-The following sections discuss the differential equations solved in the laminar and ration are also outlined,

Laminar Solution

The relations are obtained by examining exact solutions for the This momentum integral equation is derived as follows in the Cohen-Reshotko reference (ref. 4): Prandtl's boundary-layer equations are parameters related to wall shear, surface heat transfer, and free-stream velocity graincompressible laminar boundary layer. A unique correlation relating the variables is transformed for compressible flow by Stewartson's transformations (ref. 10). The redient. This gives two equations with three unknowns. Thwaite's concept (ref. 11) that After the program reads input data and does preliminary calculations, the laminar sulting first-order differential equations are then expressed in terms of dimensionless these three quantities are related in a unique way without specifying a type of velocity chosen, reducing the problem to the solution of one first-order, ordinary, nonhomogeneous differential equation in terms of a free-stream velocity gradient parameter. This is equation (28) of reference 4, boundary-layer equation is solved. profile is then assumed.

$$-u_{e} \frac{d \left(\frac{n}{d U_{e}}\right)}{\frac{d X_{tr}}{d X_{tr}}} = N(n, S_{w})$$

where

U transformed free-stream velocity,
$$U_e = \frac{a_0'}{a_e} u_e = a_0' M_e$$

$$x_{tr}$$
 transformed x-coordinate, $x_{tr} = \int_0^x k_{su} \frac{a_e}{a_0'} \frac{P_e}{P_0'} dx$

N momentum parameter, a function of n and S_w

and

$$\frac{dU_e}{dx_{tr}} = a_0^0 \frac{dM_e}{dx} \frac{1}{dx_{tr}} = a_0^1 \frac{dM_e}{dx} \frac{a_0^1 P_0^1}{k_{su}^2 a_e^2 P_e}$$

For isothermal, or nearly isothermal, surfaces, the solution of equation (1) is simplified since N can be expressed as a linear function of the pressure gradient parameter (correlation number) n as follows:

$$V = A + Bn \tag{2}$$

The solution of equation (1) is then equation (32) of reference 4,

$$n = -AU_e^{-B} \frac{dU_e}{dx_{tr}} \int_0^{X_{tr}} U_e^{B-1} dx_{tr}$$
 (3)

When transformed back to physical quantities by using Stewartson's transformation, this

$$n = -AM_e^{-B} \frac{dM_e}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_e^2\right) \frac{(3\gamma - 1)/(2\gamma - 2)}{\left(1 + \frac{\gamma - 1}{2} M_e^2\right) \frac{M_e^{B - 1}}{(1 + \frac{\gamma - 1}{2} M_e^2)} d\left(\frac{x}{L}\right)}$$

When appropriate initial values of n are used, equation (4) is solved numerically along the boundary-layer surface, giving the distribution of pressure gradient parameter (or correlation number) n.

(4)

The momentum thicktransfer from $C_f R_w / N u_x$. Form factor, finally, is obtained from an experimental correlation with n, S_w , and M_e described in reference 12; δ^* follows from form factor and the heat-transfer ness is then obtained from n, the shear stress and skin friction from l, and the heat Once n is obtained at each station, the other boundary-layer and heat-transfer The shear-stress parameter l parameter, $C_f R_{\psi}/Nu_{\chi},$ are obtained through correlation with n.parameters are easily obtained. and momentum thickness.

Laminar velocity profiles are computed by the familiar Pohlhausen technique described in reference 7.

Turbulent Solution

The momentum integral The equations derived in the Sasman-Cresci reference (ref. 5) are the momentum and moment-of-momentum integral boundary-layer equations.

The moment-of-momentum integral equation is obtained in somewhat the same way, after tion is then integrated across the boundary layer to give the momentum integral equation. The general proequation is obtained by applying a Mager-type transformation (ref. 13) to Frandtl's equa-The momentum equacedure of reference 14 is used to reduce the resulting equation to manageable form. the momentum equation is multiplied by the transformed y-coordinate. tions in which flow variables appear as time-averaged quantities. The two derived integral equations are the following:

$$\frac{d\theta_{tr}}{d\mathbf{x}_{tr}} + \frac{\theta_{tr}}{U_e} \frac{dU_e}{d\mathbf{x}_{tr}} \left[2 + \mathbf{H}_i + \frac{\delta}{0} \left(\frac{\mathbf{h}'}{\mathbf{h}'_0} - 1 \right) d\mathbf{Y}_{tr} \right] = \left(\frac{T_0}{T_e} \right) \left(\frac{T}{T_0} \right) \left(\frac{T}{T_0} \right) \frac{\tau_w}{\rho_e U_e^2}$$
(5)

and

$$\frac{dH_{i}}{dx_{tr}} = \frac{-1}{U_{e}} \frac{dU_{e}}{dx_{tr}} \left[\frac{H_{i}(H_{i}+1)^{2}(H_{i}-1)}{2} \right] \left[1 + \frac{2}{(H_{i}+1)^{\theta}tr} \int_{0}^{\delta_{tr}} \left(\frac{h'}{h'_{0}} - 1 \right) dX_{tr} \right]$$

$$\frac{2(H_{1}-1)}{H_{1}^{2}(H_{1}+1)\theta_{tr}^{2}} \int_{0}^{\delta_{tr}} \left(\frac{h'}{h_{0}}-1\right) Y_{tr} \, dY_{tr} \right] \\ + \frac{H_{1}(H_{1}^{2}-1)}{\theta_{tr}} \left(\frac{T_{0}^{i}}{T_{e}}\right) \left(\frac{T}{T_{0}^{i}}\right) \left(\frac{T}{T_{0}^{i}}\right) \frac{\tau_{w}}{\rho_{e} U_{e}^{2}}$$

$$\frac{(H_i^2 - 1)(H_i + 1)}{\theta_{tr}} \left(\frac{T_0^0}{T_e}\right) \left(\frac{T}{T_0^0}\right) \frac{\tau_w}{\rho_e U_e^2} \qquad \begin{pmatrix} 1 \\ \frac{\tau}{w} & d \left(\frac{Y_{tr}}{\delta_{tr}}\right) \\ \frac{\tau_w}{\sigma_b} & \left(\frac{Y_{tr}}{\delta_{tr}}\right) \end{pmatrix} \tag{6}$$

where

$$U_e$$
 transformed free-stream velocity, $U_e = \frac{a_0'}{a_e} u_e = a_0' M_e$

$$X_{tr}$$
 transformed x-coordinate, $X_{tr} = \int_0^x \frac{T_0^i}{T} \left(\frac{T_e}{T_0^i}\right) (\gamma+1)/(2\gamma-2)$ dx

$$Y_{tr}$$
 transformed y-coordinate, $Y_{tr} = \left(\frac{T_e}{T_0^i}\right)^{1/2} \int_0^y \frac{\rho}{\rho_0} dy$

$$\theta_{\rm tr}$$
 transformed momentum thickness, $\theta_{\rm tr} = \int_0^{\delta_{\rm tr}} \frac{{\rm U}}{{\rm U}_{\rm e}} \left(1 - \frac{{\rm U}}{{\rm U}_{\rm e}}\right) {\rm d}{\rm Y}_{\rm tr}$

transformed form factor for adiabatic flow,
$$H_i = \frac{\int_0^{t_1} \left(1 - \frac{U}{U_e}\right) dV_{tr}}{\theta_{tr}}$$

H,

tion (ref. 15), transformed for compressible flow, is used for the shear-stress terms in With Equations (5) and (6) are not in solvable form, however. Reference 5 makes use of thalpy integrals in both equations (5) and (6). The Ludwieg-Tillmann skin friction relaboth equations. And, finally, the normalized shear distribution integral of equation (6) Crocco's relation and a power-law assumption for velocity profiles to evaluate the enis evaluated by using the results of equilibrium turbulent boundary-layer analysis. these substitutions and the relation

$$f = \left(\frac{U_e \theta_{tr}}{\nu_0^4}\right)^{1.268} = \left(\frac{M_e a_0^4 \theta_{tr}}{\nu_0^4}\right)^{1.268} \tag{7}$$

equations (5) and (6) can be put into the following form:

$$\frac{\mathrm{d}f}{\mathrm{d}x} = 1.268 \left\{ \frac{-f}{\mathrm{M_e}} \frac{\mathrm{d}M_e}{\mathrm{d}x} \left[\mathbf{I} + (1 + S_{\mathrm{w}})H_{\mathrm{i}} \right] + A \right\}$$
(8)

$$\frac{\mathrm{M}_1}{\mathrm{dx}} = \frac{-1}{2\mathrm{M}_e} \frac{\mathrm{dM}_e}{\mathrm{dx}} \left[H_1(H_1+1)^2 (H_1-1) \right] \left[1 + S_w \frac{H_1^2 + 4H_1 - 1}{(H_1+1)(H_1+3)} \right]$$

$$+\frac{H_{i}^{2}-1}{f}A\left[H_{i}-\frac{0.011(H_{i}+1)(H_{i}-1)^{2}}{H_{i}^{2}}\frac{2}{C_{f}}\frac{T_{0}^{i}}{T}\right]$$
(9)

where

A = 0.123 e
$$-1.561 \text{ H}_1 \left(\frac{M_e a_0^4}{\nu_0^4} \right) \frac{T_e}{T} \left(\frac{T_e}{T_0^6} \right)^{(\gamma+1)/(2\gamma-2)} \left(\frac{\mu}{\mu_0^4} \right)^{0.268}$$

and

$$\frac{c_{f}}{2} = \frac{\tau_{w}}{\rho_{e} u_{e}^{2}} = 0.123 e^{-1.561 H_{1}} \quad f^{-0.2113} \left(\frac{T_{e}}{T}\right) \left(\frac{\mu}{\mu_{0}}\right)^{0.268}$$

uncoupled in the Sasman-Cresci method as they were in Reshotko and Tucker's analysis. which govern the development of the turbulent boundary layer. These equations are not Equations (8) and (9) are the coupled, first-order, ordinary differential equations

Using initial values calculated in the laminar routine or given by the user, equations Turbulent velocity profiles are calculated by means of the power law along the surface. The usual boundary-layer parameters are then obtained from these (8) and (9) are solved by a Runge-Kutta scheme, giving the distribution of f and H_i two distributions.

Transition

prediction of transition from laminar to turbulent flow. Details of the method are sum-The Schlichting-Ulrich-Granville method (refs. 8 and 9) is used for the theoretical marized in reference 7.

curves of neutral stability (see ref. 7) for laminar boundary layers in various pressure Schlichting and Ulrich used sixth-degree Pohlhausen velocity profiles to calculate

gradients. From these curves, a single curve of critical momentum-thickness Reynolds the point of instability and the point of transition is predicted by means of an experimen-Pohlhausen parameter \overline{K} . Once an instability point is located, \overline{K} can be calculated and predicting the point of instability of the laminar boundary layer. The distance between This curve is used by the program for tal curve by Granville. This curve represents the difference in momentum-thickness Reynolds numbers at the instability and transition points plotted against a mean number against shape factor K was obtained. the location of transition determined.

Separation

the station where skin friction coefficient $\, {
m C}_{
m f} \,$ or wall shear stress $\, au_{
m W} \,$ passes from posseparation station and the previous station in order to more exactly determine the point Laminar case. - In the laminar boundary layer, separation is assumed to occur at at the itive to negative, indicating backflow. The user should check the values of $\,C_{
m f}$ of separation.

This is a relatively high value for H_{i} , and H_{i} grows rapidly near separation. The valare printed at each output station and at each point where the turbulent differ-Turbulent case. - In the turbulent boundary layer, separation is predicted based on the magnitude of $H_{\mathbf{i}}$. (The turbulent equations do not allow a negative $C_{\mathbf{f}}$.) Separation is predicted by the program at the station where H₁ achieves a value greater than 2.8. ential equations are solved. If the user feels that a lower value of $\mathbf{H_i}$ is more appropriate for separation (2.0 to 2.5 is typical), a different separation point can be chosen from these printed values. ues of H_i

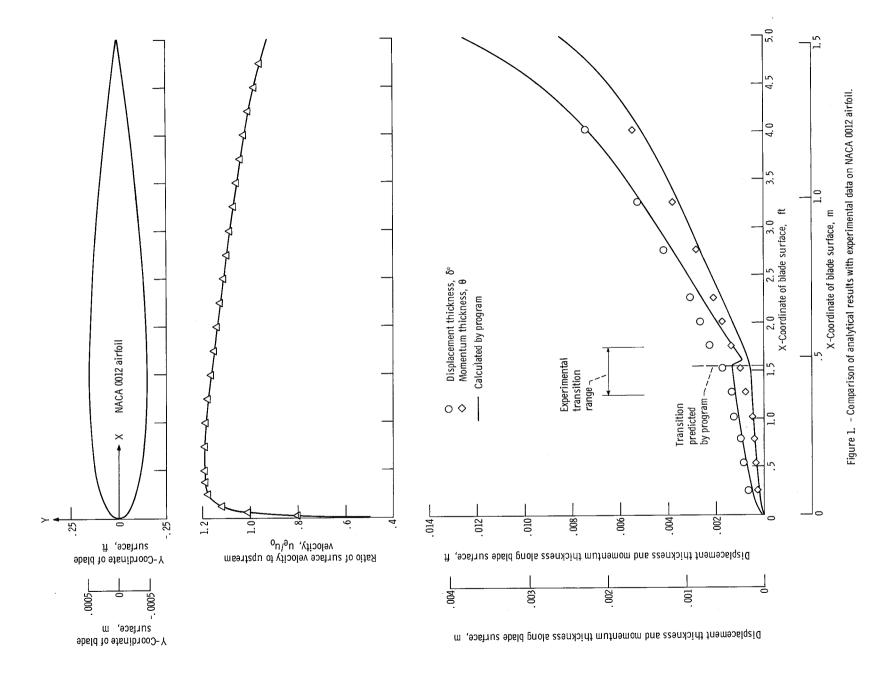
Another way of predicting turbulent separation is to plot the output distribution of $\,{
m C_{
m f}}$ as a function of X. The separation point is then predicted by extrapolating C_{f} to zero. The extrapolation should be started where C_f is falling rapidly and continued to zero without a point of inflection.

NUMERICAL EXAMPLES

of initial values of displacement and momentum thickness at the beginning of the boundary The first is an NACA airfoil which has both laminar and turbulent boundary layers, and the second is a converging-diverging channel with turbulent boundary layer throughout. The airfoil illustrates the prediction of transition by the program, and the channel illustrates the use Two numerical examples are given to illustrate the use of the program. layer. In both cases the computer input is included.

TABLE I. - INPUT FOR NACA 0012 AIRFOIL

							E 16 • 11 E	0.0000	60000 °S
							322, 062	55040.0	00051.4
							336,857	0.07240	00005.4
							869.866	0.10275	4.25000
					0000		345.743	51181.0	4.00000
							351*158	C • I 2802	3.75000
							326.230	0.18320	3.50000
							868 * 39£	58902.0	3,25000
							ϧ 9ε•39ε	0.22815	3.0000
							376,100	09745.0	2.75000
							9 EB • PT E	07792.0	S* 20000
					0000	*009 00	T 64.9TE	2067S.0	00052.5
					0000	*009 00	179.585	51062*0	S* C0000
					0000	*009 00	8 55 •83 5	0.29735	1.75000
					0000	*009 00	⊊8 ≯° 58€	0.29825	1. 70000
					0000	*009 00	86 6. 366	00662*0	00059*1
					0000	*309 00	391.312	09567*0	1. 60000
					0000	*309 00	365°55	95562*0	00055 *1
					0000	*309 30	501.°E5E	01008-0	1* 20000
					0000	*009 00	0 96 ° 85 8	96662.0	00057°t
					0000	*309 00	96L ° 76 E	09562*0	1.40000
					0000	*009 00	715°56E	05857*0	1.35000
							986.958	01867*0	1. 30000
							791°L6E	6.29705	1.25000
							400,209	C*S8982	1.00000
							006 * 10 5	0.26725	000SL *0
							006*10+	617870	00009 0
							466.394	C*S1000	00975.0
							791°46E	9LLL1.0	00052.0
							998.975	57051.)	0.12500
							766 *5 £ £	07400.0	0.56250
							0 79 * 3 L Z	69780.0	0.6550
						*309	•3	• 5	•0
						MI	∃n	٨	х
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				τ	ī	1	. 1	1	ı
				къван	KWAIN	KFVW	k≥ĎE	KGBVD	КЬВЕ
				30007	MIAWA	W 1/1	2037	G T G D M	200%
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						GGHII	841114	WV 11	H
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CIHET	KATCH	Kre	KZbſИ	KSWTH	KE₩	КРУМ	аялти	чVР	1 SN
					0+82.0	00*009	30*S+97	84.3171	1.400
					UFMACH	211	21 d	В	Ø ∀9
						0.0=10 0.0	CV 0015 C=	(MBF-685) NV	BE CK EB



NACA 0012 Airfoil

etry, surface velocity distribution, and comparison of output with experimental results is The blade geomfree-stream inlet Mach number is 0.284. The configuration listed in reference 16 had a The first example is an NACA 0012 airfoil at zero angle of attack (ref. 16). chord length of 5.0 feet. The input for this example is given in table I. given in figure 1.

The boundary layer was assumed to begin at a stagnation point at the leading edge of are compared with experimental values in figure 1. The agreement is good except for a region around the transition point. This is understandable since transition occurs gradstronger concentration of input points was given in the transition range so that the point of transition could be located more precisely (see table I). Output values of δ^* and θ the blade, and no initial values were used. Transition was predicted naturally by the program, and occurred within the range in which it was measured experimentally. ually in the actual flow, but is forced to occur at a single point in the program.

Execution time for this program was 0.4 minute.

Converging-Diverging Channel

The second example is a two-dimensional channel in which the flow is turbulent. The were taken at Lewis but have not previously been reported. The input for the curved wall of this example is given in table II. The wall pressure distributions, and comparison of upper wall of the channel converges and diverges and the bottom wall is flat (see fig. 2). Boundary layers were computed on both walls. Experimental data on this configuration output for both walls with experimental data, are given in figure 2.

on the measured velocity profiles. The values of δ used in the integrations to calculate free-stream flow at these points, it was difficult to locate the edge of the boundary layer ary layer was started at the initial station. Agreement between measured and predicted On both surfaces, initial values were given for δ^* and θ , and the turbulent boundvalues on the flat wall is extremely good. On the curved wall, agreement is also good. diverging portion of the curved wall. Because of the curvature of streamlines in the θ on the converging-There is some doubt about the experimental values of δ^* and θ may have been conservative.

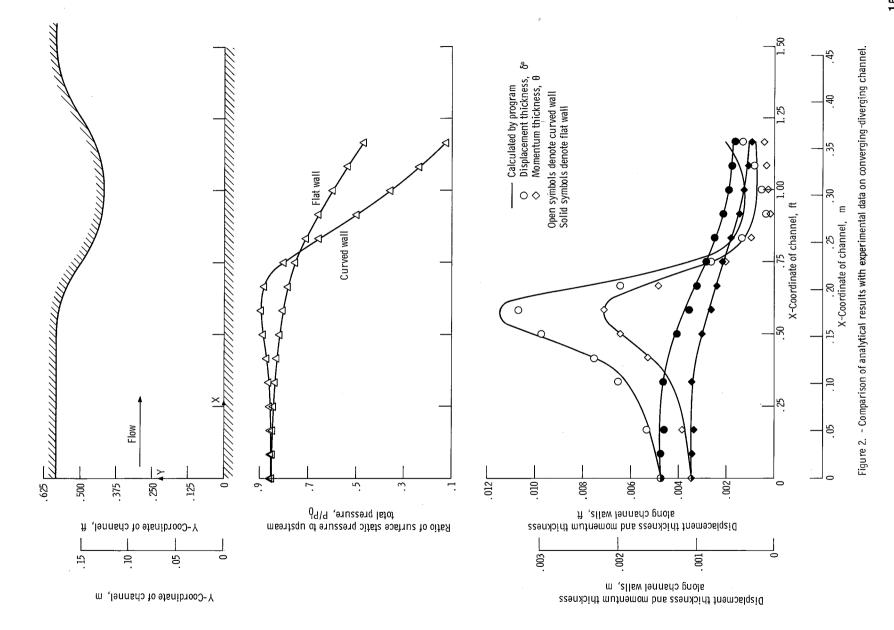


TABLE II. - INPUT FOR CURVED-WALL CHANNEL

COSAED MALL - DRY AIR

					H28M4C 1.584.0	235*00 115	77.400S	8 ÷. 917 1	00 5°1 8∀9
*0 19 F1 0	KATS4	0 KFZ	0 N7dS>	HIM2> C	Э КЕW	+ КЬЛШ	NTURB I	qVN CΙ	5 T 1 S N
						11URB 0.003420	01088 0.004710	### •0	°0 DF∀4
				7 7	KMAIN	ĭ KF∀W	I K 2DE	I K€K∀O	I Kbke
						JAWT CO.SE2	21409 000538 . 0	00E85*0	x •0
						235*00	00874800	00585.0	0.5880.0
						CO * ZES	001558*0	00685.0	0.07 31.0
					CC	235 *00	008858.0	00885.0	0.00 25 00
						532.00	0.862300	กกรคร • ก	00888.0
						C0.552	004178.0	00283 0	07617.0
						00.258	0089688*0	00£82 . 0	0.0002 0
						CO*285	000788*0 008968*0	00845.0	0.07.55.0
						632.00	000008 • 0	00764.0	0.0027.0
						532.03	0.0653000	00157*0	0.08.88.0
						6925.00	0.00864.0	00524.0	01916.0
					cc	235*00	0009980	01914.0	1.00000
						632.00	0.00255.0	00624.0	1.08330
					CC	635.00	0.021.0	001550	1.16700

INPUT

Further The first may put whatever information he wishes in order to identify the data deck. The remainexplanation of the proper preparation of input is given in the section Special Instructions In any of the columns from 1 to 80 of this card, the user These are defined in the 'dictionary'' below. Figure 3 shows the input variables as they are punched on the data cards. ing cards are for input variables. input data card is for a title. for Preparing Input (p. 20).

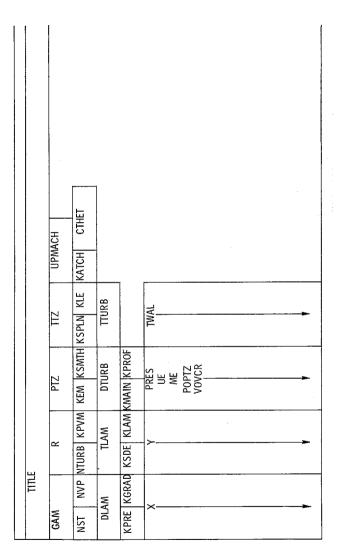


Figure 3. - Input form.

Dictionary of Input Variables

After a title card, the following input variables are given:

GAM specific-heat ratio, γ

universal gas constant, \mathcal{A} , $(\mathrm{ft})(\mathrm{lbf})/(\mathrm{slug})(^{0}\mathrm{R})$; $\mathrm{J/(kg)(K)}$ \mathbf{z}

inlet or upstream relative total pressure (station 0), P_0 , $\mathrm{lbf/ft}^2$; $\mathrm{N/m}^2$ PTZ

inlet or upstream relative total temperature (station 0), T_0^{\prime} , O R; K TTZ

inlet or upstream Mach number relative to surface, $\,\mathrm{M}_{0}$ UPMACH

NST	integer number of input stations (≤ 100) along boundary-layer surface
NVP	integer number of points desired in velocity profile at each station
NTURB	integer number of station, if any, at which user wishes turbulent boundary layer to begin (NTURB is usually zero, allowing program to calculate position of transition to turbulent boundary layer. NTURB may also be given any value from 1 to NST. If NTURB = 1, initial values must be given for DTURB and TTURB. If NTURB > 1, initial values may or may not be given.)
KPVM	integer from 1 to 5 indicating which form of surface flow distribution is given as input: Pressure
KEM	integer (0 to 1) indicating which of the two allowable sets of units are used in input: English (pounds force, slugs, feet, seconds, degrees Rankine, and foot-pounds)
KSMTH	integer $(0,\ 1,\ 2,\ \ldots)$ indicating number of times distribution of freestream velocity is to be smoothed prior to computation of surface gradients
KSPLN	integer (0 or 1) indicating manner in which surface gradients are to be calculated: Weighted-difference technique
KLE	integer (0 to 1) indicating type of initial condition existing at station 1: Stagnation point or initial values given
KATCH	integer (0 or 1) indicating whether laminar-boundary-layer separation (if encountered) should reattach as a turbulent boundary layer: Separation and stop

1 2 8 4 5

CTHET	real variable used when KATCH = 1, indicating ratio of momentum thickness after reattachment to momentum thickness at laminar separation
DLAM	initial displacement thickness, if any, of laminar boundary layer at station 1, ft; m (DLAM may be zero or have some finite value.)
TLAM	initial momentum thickness, if any, of laminar boundary layer at station 1, ft; m (TLAM may be zero or have some finite value.)
DTURB	initial displacement thickness, if any, of turbulent boundary layer, ft; m (DTURB may be given for station designated by NTURB, or for station at which transition is calculated by program.)
TTURB	initial momentum thickness, if any, of turbulent boundary layer, ft; m (see DTURB)
KPRE	integer (0 or 1) indicating whether printing of output from PRECAL is desired (see OUTPUT): Output suppressed
KGRAD	integer (0 or 1, see KPRE) indicating whether printing of surface gradients of velocity and Mach number is desired (see OUTPUT)
KSDE	integer (0 or 1, see KPRE) indicating whether printing of solutions of laminar and turbulent differential equations is desired (see OUTPUT)
KLAM	integer (0 or 1, see KPRE) indicating whether printing of laminar calculations for location of instability and transition is desired (see OUTPUT)
KMAIN	integer (0 or 1, see KPRE) indicating whether printing of principal calculated boundary-layer parameters is desired (see OUTPUT)
KPROF	integer (0 or 1, see KPRE) indicating whether printing of velocity profiles is desired (see OUTPUT)
×	array of X-coordinates of input stations, ft; m (see figs. 4 and 5)
Y	array of Y-coordinates of input stations, ft; m (see figs. 4 and 5)
PRES	array of static pressure P at X-Y input stations, $1\mathrm{bf/ft}^2$; $\mathrm{N/m}^2$
UE	array of free-stream velocities $\mathbf{u}_{\mathbf{e}}$ relative to surface at X-Y input stations, ft/sec; m/sec

M_e relative to surface at X-Y input array of free-stream Mach numbers stations ME

atarray of ratios of static pressure to relative total pressure $\mathrm{P}/\mathrm{P}_0^{"}$ X-Y input stations POPTZ

ocities $u_e/u_{\rm cr}$ at X-Y input stations $(u_{\rm cr}$ is the speed of sound at Mach 1, and is only a function of relative total temperature.) array of ratios of relative free-stream velocities to relative critical vel-VOVCR

$$u_{Cr} = \sqrt{\frac{2\gamma R}{\gamma + 1}} T_0'$$
 (10)

array of static wall temperatures at X-Y input stations, ⁰R; K (If TWAL is unknown and surface is nearly isothermal, the value of TTZ may be used for TWAL.)

Special Instructions for Preparing Input

(velocity, etc.) and wall temperature are given, and at which boundary-layer parameters scribe the surface geometry (see figs. 4 and 5). These are the points at which pressure - The X and Y input arrays give coordinates of points which de-Surface geometry.

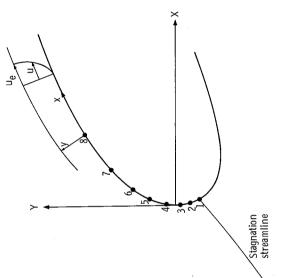


Figure 4. - Coordinate systems for geometry input and boundary-layer output on a blade surface.

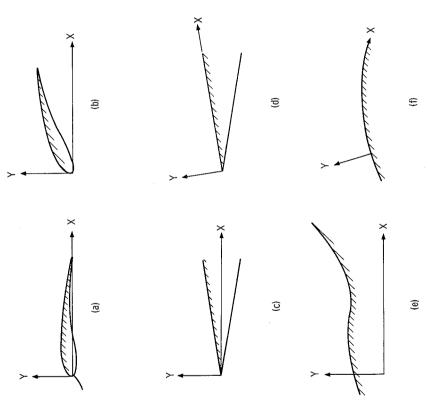


Figure 5. - Variation in placement of X-Y coordinate system.

will be given as output. Enough points (20 or 30 is typical) should be given so that surface length (used in the calculation of surface velocity gradients) can be calculated with reasonable accuracy from the formula

$$x_{j} = x_{j-1} + \sqrt{(X_{j} - X_{j-1})^{2} + (Y_{j} - Y_{j-1})^{2}}$$
(11)

More points should be concentrated in areas where surface curvature is high; not only so that surface length is accurate, but because it is in these regions where velocity gradients will change most rapidly.

layer surface. The origin and orientation of these axes are completely arbitrary, since These axes can also be curvilinear (with Y = 0 everywhere), Figure 5 shows some ways in which the X-Y axes can be related to the boundarythe X-Y coordinates are only used to identify the surface points and compute surface agreeing with the boundary-layer axes x and y (see fig. 5(f)). length by formula (11).

Leading-edge conditions. - There are two principal leading-edge conditions: a stag-

nation point at station 1 (KLE = 0), or a sharp or pointed leading edge at station 1 (KLE=1).

used, and initial values where they are known are given for DLAM, or TLAM, or DTURB The program will also accept data which begin at some point within the boundary layer other than the starting point of the boundary layer. In these cases, KLE = 0and TTURB.

Inlet conditions. - PTZ, TTZ, and UPMACH (P_0', T_0', M_0) should be given at a reffig. 6) where the flow is not affected by the boundary layer. Free-stream Mach number $m M_{0}$ is not a critical input; it is used to obtain static temperature, from which Prandtl erence point outside the boundary layer or in the free stream opposite station 1 (see number and thermal conductivity are obtained by means of curve fits.

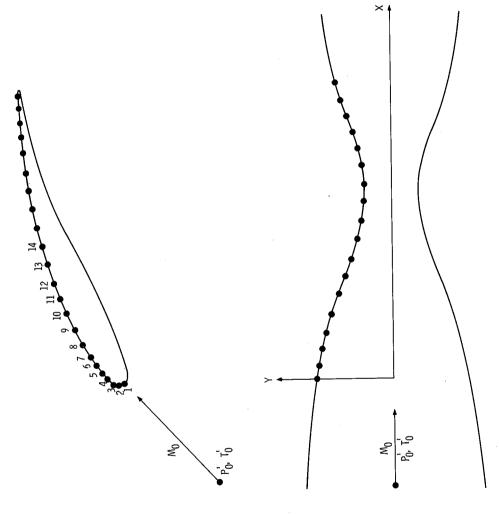


Figure 6. - Location of typical upstream input conditions.

accurately. Also, since answers are only printed at points where input was given, enough pressure, or ratio of free-stream velocity to free-stream critical velocity. Enough input points (<100) should be used (especially in areas where surface curvature is high or distribution of pressure changes rapidly) so that gradients of velocity will be computed pressure, free-stream velocity, free-stream Mach number, ratio of pressure to total - Any one of five parameters may be used as input to describe flow along the boundary-layer surface: Surface distributions of pressure, velocity, and Mach number. points should be used to satisfy the requirements for output.

tions of pressure (or velocity, etc.). These gradients are a function of the smoothness of smooth his input data whenever necessary. (An examination of the gradients computed by the input distributions. Distributions of pressure calculated from experimental readings or read from a plot of pressure tend to be less smooth than those computed analytically. Smoothing of surface distributions. - The velocity and Mach number gradients used the program will indicate whether smoothing is required on a subsequent run.) Smoothin the solution of the boundary-layer equations are computed from the surface distribu-The user must therefore use his judgement and, by setting KSMTH = 1, 2, \dots , etc., ing affects peaks and valleys most strongly, the effect diminishing as more points are used to describe the peak or valley.

difference method (see subroutine GRADNT) using weighted slopes between each point and adjacent points to compute slope at each reference point. The second method (KSPLN=1) fits a spline curve to the data in order to compute slopes. The latter method gives more when using the spline since it forces the curve fit to pass exactly through each data point. The computed velocity and Mach number gradients should be checked in the program outaccurate results when the data are very smooth. Caution should be exercised, however, the input data should be smoothed, or the weighted slope method (KSPLN = 0) should be Calculation of surface gradients. - Surface gradients of velocity and Mach number The first (KSPLN = 0) is a put when the spline fit is used. If these gradients are oscillating in magnitude or sign, can be computed by two different methods in the program.

tion will be forced to occur at the station specified by that number, even if the Schlichting-Arbitrary selection of transition point. - Ordinarily the point of transition is calculated by the Schlichting-Granville method. However, the user can control this point by means of the variable NTURB. If NTURB is given a number greater than zero, transi-Granville method would have predicted it sooner, or later, than that station.

values are not given to DTURB and TTURB, laminar values of displacement and momen-If he does so, they are used at the station specified by NTURB. If the user gives a value to NTURB, he may or may not choose to give values to tum thickness at the station specified by NTURB are used as initial values. (When NTURB = 1, however, values must be given for DTURB and TTURB.) DTURB and TTURB.

turbulent values are used at the station specified by NTURB, or (when NTURB = 0) at the If initial turbulent values are given, both DTURB and - The user may give initial values whenever he knows them. In the laminar case, only one value is required (either DLAM or TLAM). TTURB must be given. Initial laminar values, if given, are used at station 1. Initial θ. station where transition is predicted. Use of initial values of δ^* and If both are given, TLAM is used.

final laminar momentum thickness by CTHET and uses this as an initial value for starting Laminar separation and reattachment. - The user may simulate laminar separation and reattachment by use of the variables KATCH and CTHET. Ordinarily the program However, if laminar separation is located and KATCH = 1, the program multiplies the stops calculating when it locates either laminar or turbulent separation at any station. the turbulent boundary layer at that point.

- Either English or metric units may be used for input and each type of units may be used. If English units are used (KEM = 0), they must be the output. However, due to certain curve fits in the program, only one consistent set of English or metric units. following:

```
Force, 1bf
Length, ft
Time, sec
Mass, slug (or (1bf)(sec<sup>2</sup>)/ft)
Temperature, <sup>O</sup>R
```

If metric units are used (KEM = 1), they are as follows:

```
Force, N
Length, m
Time, sec
Mass, kg (or N-\sec^2/m)
```

Temperature, K

Since either of these two sets of units can be employed, the output is not labeled with any A has units of energy per unit mass per degree. With these consistent sets of units, density is mass per unit volume, energy is force times distance, and the gas constant

fields (see fig. 3). They must all be right adjusted. The input variables on all other data Format for input data. - All the numbers (except CTHET) on the card beginning with NST and on the card beginning with KPRE are integers (no decimal point) in five-column cards are real numbers (punch decimal point) in 10-column fields.

OIITPIIT

Most of the output is optional and is controlled by the input card which begins with KPRE. In most cases, output labels agree with internal variable names which are defined in the output would be lengthy, so only a few lines from each section are included in the table. The entire Sample output for the NACA 0012 airfoil example is given in table III. DICTIONARY OF VARIABLES IN MAIN SUBROUTINES.

Each section of output in table III has been numbered to correspond to the following

- matically. All items are labeled as on the input form (fig. 3). In this example, velocity (1) Output numbered 1 is a listing of the input data, which is always printed auto-(UE) has been used to describe flow along the surface.
- scribing flow along the surface (PRES, ME, POPTZ, and VOVCR), geometrical variables (2) Output numbered 2 corresponds to KPRE. It includes the other four variables dethe wall (RW = $u_e x/\nu_w$), and local density distributions (RHSW and RHSE). These are all temperature distributions (TSE, TAWL, TAWT, and TBAR), local Reynolds number at (S, XOM, YOM, and SOL), local speed of sound (AE), static, recovery, and reference variables which are used in the calculation of the boundary layer. If any smoothing is done, smoothed distributions of the five variables describing pressure and velocity (PRES, UE, ME, POPTZ, and VOVCR) are also included here.
 - DMDL = $dM_e/d(x/L)$) computed by either the weighted-slope method or the spline curve-(3) Output numbered 3 corresponds to KGRAD. It contains the three gradients of velocity and Mach number along the surface (DUDS = du_e/dx , DMDS = dM_e/dx , and
- compressible form factor (FORMI), and a function (F) of the momentum thickness. These (4) Output numbered 4 corresponds to KSDE. It contains the numerical solutions of the laminar and turbulent differential boundary-layer equations. In the laminar case, the solution is correlation number (CORLN). In the turbulent case, the solution is insolutions are printed with respect to the surface length x.
 - ables, RTHI (increasing from station to station) and RCRIT and RTRAN (decreasing from station to station), are used in this analysis. When RTHI grows larger than RCRIT, in-(5) Output numbered 5 corresponds to KLAM. It contains the variables used in the stability has occurred. When RTHI bypasses RTRAN, transition is assumed to occur. laminar subroutine to check for position of instability and transition. The three vari-

times indicates that instability or transition occurs closer to the previous station than the indicated station. Since final answers for turbulent thickness parameters are affected by RCRIT or RTRAN, respectively. Examination of the values of RCRIT and RTRAN some-Instability and transition stations are located no matter how far RTHI has gone past

the station at which transition occurs, the user may wish to rerun the program with additional points in this area so as to locate transition more exactly.

- layer thickness (DELTA), displacement thickness (DELSR), momentum thickness (THET), and turbulent boundary layers, and the stations at which instability, transition, and sepamomentum-thickness Reynolds number (RTH). It also contains the heat-transfer paramration occur. It contains all the principal boundary-layer output parameters: boundary-(6) Output numbered 6 corresponds to KMAIN. It indicates the regions of laminar form factors (FORM and FORMI), skin friction parameters (CF and TAUW), and eters (DTDY, NUSS, HTRAN, and CRN).
 - each of the stations along the surface. Profiles (U/UE) are given at equally spaced in-(7) Output numbered 7 corresponds to KPROF. It contains the velocity profiles at crements of distance (Y/DELTA) away from the surface.

TABLE III. - SAMPLE OUTPUT

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EYELISH UNITS USED FOR INPUT AND QUIPUL.

TABLE III. - Continued. SAMPLE OUTPUT

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TABLE III. - Continued. SAMPLEOUTPUT

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105°1 825°1 825°1 696°1 451°2 45	-3.0516 -3.1360 -3.094	15*199 25*099 91*755 66*809 66*809 66*196 65*196 76*816 15*207 00*951 00 SSAN	YQTO YQTO O YQTO YQTO O YQTO O YQTO O YQTO O YQTO O YQTO O YQTO O	HTS 4.501 6.601 6.608 6.40	#\$#\$0.0 #\$#\$0.0 #\$#\$0.0 #\$#\$1.0 #\$\$1.0 #\$1	9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0 9000.0	VOLIANZ
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	.600	.351308E-0	.702616F	49.7	.922
	650	.3805845-0	.761168F-	56.4	.947
	750	440 5 860F-0	.819719F	61.5	996.
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	.850	.497687F-0	. 995373F-0	4.69	995
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	001.	.5161658-0	103233E-0	58.3	.660
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	• 300	.154850F-0	309699F-0	14.9	834
	• 350	.1AC65AE-0	361316E-0	23.8	.827
	400	.206466F-0	412932F-0	31.7	.847
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	.650	3355085-0	671015F-0	62.0	.925
	200	361316E-U	/22632F-0	66.99	.937
	800	4129325-0	7 74 Z48 F=0 8 2 5 8 6 5 F=0	75.8	944
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ERROR CONDITIONS

This section lists the error messages given by the program and tells what to do when they are encountered:

RECHECK INPUT INSTRUCTIONS. (1) ERROR IN INPUT DATA. This message is printed by subroutine INPUT if one of the following conditions is not met:

(2) THERE IS A STAGNATION POINT AT A STATION OTHER THAN STATION THIS IS NOT ALLOWED,

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This message is printed by subroutine PRECAL if any of the following conditions is met at a station other than station 1:

$$P = P_0^{\dagger}$$
 $u_0 = 0$.
 $M_0 = 0$.
 $P/P_0 = 1$.
 $e/u_{Cr} = 0$.

If a stagnation point occurs in the input pressure or velocity distribution, it must occur at station 1.

THAN ZERO OR GREATER THAN ITS MAXIMUM ALLOWABLE VALUE (3) AN INPUT PRESSURE, VELOCITY, OR MACH NUMBER IS EITHER LESS

This message is printed in subroutine PRECAL if any of the following conditions is met at any station:

$$P < 0$$
. or $P > P'_0$
 $u_e < 0$.
 $M_e < 0$.
 $P/P'_0 < 0$. or $P/P'_0 > 1$.
 $u_e/u_{cr} < 0$. or $u_e/u_{cr} > \sqrt{(\gamma + 1)/(\gamma - 1)}$

(4) A NEGATIVE INITIAL VALUE HAS BEEN GIVEN. THIS IS NOT ALLOWED,

This message is printed by subroutine LAMNAR if one of the four initial values (DLAM, TLAM, DTURB, or TTURB) is less than zero. They can be positive or zero, but not negative.

(5) INITIAL VALUES WERE NOT GIVEN FOR THE TURBULENT BOUNDARY LAYER AT STATION 1.

for both DTURB and TTURB. If the turbulent boundary layer is to start at station 1, ini-This message is printed by subroutine LAMNAR if NTURB = 1 and values are not given tial values must be given for both displacement thickness and momentum thickness.

(6) INITIAL VALUES WERE GIVEN FOR THE TURBULENT BOUNDARY LAYER AT A STAGNATION POINT.

have been given values, but the pressure, velocity, or Mach number at station 1 indicates This message is printed by subroutine LAMNAR if NTURB = 1 and DTURB and TTURB A pressure less than $P_0^{\mbox{\tiny !}}$, or a velocity or Mach The program will not allow a turbulent boundary number greater than zero, should be given for this case at station 1. layer to begin at a stagnation point. a stagnation condition at that point.

(7) INITIAL VALUES OTHER THAN ZERO WERE GIVEN FOR THE LAMINAR BOUNDARY LAYER AT A STAGNATION POINT.

and/or TLAM but the pressure, velocity, or Mach number at station 1 indicates a stagnagreater than zero, should be given at station 1 if the laminar boundary layer has a thick-This message is printed by subroutine LAMNAR if initial values are given for DLAM tion condition at that point. A pressure less than P_0^{\prime} , or a velocity or Mach number

PRESSURE SHOULD DECREASE INITIALLY. EITHER GIVE AN INITIAL VALUE FOR DISPLACEMENT OR MOMENTUM THICKNESS, OR BEGIN POINT, SINCE NO INITIAL THICKNESSES ARE GIVEN. IN THIS CASE (8) FOR THIS INPUT DATA STATION 1 IS ASSUMED TO BE A STAGNATION WITH A SHORT REGION OF FAVORABLE PRESSURE GRADIENT. This message is printed by subroutine LAMNAR. If initial values are not given, and input does not indicate a sharp leading edge, the program assumes it has a stagntion point or M_e = 0). However, the program will accept other values of pressure or velocity at The initial pressure ordinarily given in this case would be P_0^{\prime} (or u_e station 1, as long as $\,dP/dx<0\,$ initially. at station 1.

(9) LAMINAR SOLUTION HAS PROCEEDED BEYOND THE RANGE WHERE IT IS VALID.

tions should be used to pass through any rapid change in pressure or velocity distribution. This message is printed by subroutine LAMNAR if the value of correlation number calculated in the solution of the laminar-boundary-layer equation is beyond the range $-0.32 \le$ $n \leq 0.16$. This can be caused by a strong adverse or favorable pressure gradient, generally occurring rapidly over one or two stations along the surface. Several input sta-

(10) IF INITIAL TURBULENT VALUES ARE GIVEN, THEY BOTH MUST BE NONZERO

This message is printed by subroutine LAMNAR if one of the following conditions exists:

If initial values are given for the turbulent boundary layer at any station, $rac{\mathrm{both}}{\mathrm{th}}$ displacement thickness and momentum thickness must be given.

(11) ERROR IN COMPUTING INTEGRAL FOR CORLN or ERROR IN COMPUTING INTEGRAL FOR KBAR.

the SIMPS1 integration routine. This condition should generally not occur with the kinds One of these messages is printed by subroutine LAMNAR if an error occurs in a call on of distributions being integrated in this program.

INFORMATION FOR PROGRAMMER

DESCRIPTION OF PROGRAM

The program BLAYER is segmented into five principal parts; the subroutines INPUT, These, in turn, call several other sub-All the subroutines and their relation are shown in figure 7. PRECAL, LAMNAR, TURBLN, and PROFIL. routines.

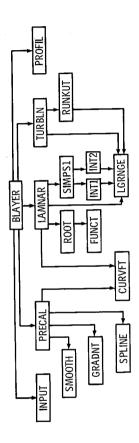


Figure 7. - Calling relation of program subroutines.

These are all in The remaining These variables are all All subroutines subroutines are described after the main dictionary in the section AUXILIARY SUBusing these variables are described in the section MAIN SUBROUTINES. Most of the subroutines in BLAYER use the same set of variables. defined in the DICTIONARY OF VARIABLES IN MAIN SUBROUTINES. Their variables are described with each subroutine. COMMON blocks which transmit information between routines. ROUTINES.

 $50511_{(8)}$ of which $24627_{(8)}$ is used in storage of variables. The main subroutines require (NST) and as many points as the user desires normal to the surface in any of the velocity profiles (NVP). The program is run at Lewis on the IBM-7094/7044 direct-coupled sys-The auxiliary The program can handle as many as 100 points along the boundary-layer surface tem with a 32 768-word core $(77777_{(8)})$. The total program storage requirement is $42305_{(8)}^{-7}$ words of storage of which $14336_{(8)}$ is used for COMMON blocks. subroutines use 6204(8) words.

the input data and checks for errors. PRECAL then calculates all quantities which remain After transition, it comboundary-layer equations by using RUNKUT, and computes the turbulent-boundary-layer putes the initial values for the turbulent boundary layer. TURBLN solves the turbulent-The subroutine LAMNAR solves the laminar differential equation, computes the constant, and are subsequently used by the laminar- and turbulent-boundary-layer rou-This reads in and prints Finally, PROFIL computes both laminar and turbulent velocity profiles. laminar-boundary-layer parameters, and checks for transition. The first principal routine called by BLAYER is INPUT.

Conventions Used in Program

at the end of a variable name refers to conditions external to the boundfers to station 0, where total conditions are given in the input; T means total conditions, represents pressure, T temperature, V velocity, A speed of sound, Thus, for example, For clarity, a number of conventions are used in naming variables in the program. ary layer, whereas W refers to conditions at the wall or boundary-layer surface; dynamic viscosity, and NU kinematic viscosity. POPTZ represents pressure over total pressure at station 0. density, MU static; P

Labeled COMMON Blocks

the variables in COMMON blocks. The labeled COMMON blocks are briefly described by The same variable names are used in the different subroutines for all Most variables which are used in more than one subroutine are placed in labeled COMMON blocks. the following:

- C1/ contains all input variables
- /C2/ contains single variables computed in PRECAL
- /C3/ contains all arrays computed in PRECAL
- contains arrays of all principal boundary-layer parameters computed in LAMNAR and TURBLN /C4/
- contains variables transferred between LAMNAR and PROFIL, and between LAMNAR and INT1 and INT2 C5/
- contains initial turbulent values transferred between LAMNAR, TURBLN, and $^{/92/}$
- contains variables indicating position of instability, transition, and separation /C1/
 - (These are contains tables for solution of turbulent boundary-layer equations transferred from RUNKUT to TURBLN.) $^{/8}$
- contains variables indicating whether transition or separation has been encountered, or whether any errors have been found $/c_{0}$

MAIN SUBROUTINES

The following subroutines are particular to the BLAYER program, and all use the

they COMMON blocks described in the previous section. More general subroutines (i.e., are independent of BLAYER) are discussed in the section AUXILIARY SUBROUTINES

Subroutine INPUT

Subroutine INPUT reads and prints all input data. It also checks for errors in the

Subroutine PRECAL

the boundary-layer differential equations. All the variables it computes remain constant Subroutine PRECAL performs all the calculations required prior to the solution of for the remainder of the program.

coefficients for these are stored into arrays at the beginning of the routine. Coefficients Reading of coefficients for curve fits. - PRECAL uses several curve fits, and the are given for the following functional relations (see appendix B):

$$\left(\frac{\mathbf{T}}{\mathbf{s}_{l}}\right) = \mathbf{f} \left(\frac{\mathbf{T}}{\mathbf{T}}\right)$$

$$\mathbf{Pr} = \mathbf{f} \left(\frac{\mathbf{T}}{\mathbf{T}_{\mathbf{S}l}} \right)$$

$$\frac{\mathrm{k}}{\mathrm{k}_{\mathrm{S}^{\prime}}} = \mathrm{f}\left(\frac{\mathrm{T}}{\mathrm{T}_{\mathrm{S}^{\prime}}}\right)$$

These relations have been nondimensionalized so that they can be used with either English or metric units.

The curve fits Geometrical parameters are also obtained, and surface - Using the total parameters and Mach number at station 0, other total and static parameters required by the program are computed. length computed from equation (11). are used in these calculations. Initial calculations.

If the user has requested smoothing, SMOOTH is then called for the velocity distribution Calculation and smoothing of surface flow distributions. - One of five possible vari-Each time smoothing is performed the other four surface distributions are recom-PRECAL, the remaining four variables are calculated from the variable given as input. ables is used as input for flow past the boundary-layer surface. In this section of

puted from UE, and all five distributions are reprinted. After surface distributions have been finalized, other constant parameters depending on them are calculated.

 $(du_e/dx, dM_e/dx, and dM_e/d(x/L))$ are calculated by means of calls on either GRADNT Calculation of surface gradients. - Surface gradients of velocity and Mach number or SPLINE, depending on which the user has requested.

Subroutine LAMNAR

putes laminar-boundary-layer parameters, checks for instability and transition to turbu-Subroutine LAMNAR solves the laminar differential boundary-layer equation, comlent flow, and computes initial values for the turbulent boundary layer when transition

routine, and the coefficients for these are stored into arrays at the beginning of the rou-Reading of coefficients for curve fits. - Several curve fits are used in the LAMNAR Coefficients are given for the following functional relations:

$$\eta_{\mathbf{S}\mathbf{p}} = f(\mathbf{S}_{\mathbf{w}})$$
 $\left(\mathbf{R}_{\theta}\right)_{\mathbf{c}\mathbf{r}} = f(\mathbf{K})$
 $\left(\mathbf{R}_{\theta}\right)_{\mathbf{i}, \Delta} = f(\overline{\mathbf{K}})$
 $\left(\frac{\mathbf{c}_{\mathbf{f}}\mathbf{R}_{\mathbf{w}}}{\mathbf{N}_{\mathbf{w}}}\right)_{\mathbf{r}=1} = f(\mathbf{n}, \mathbf{S}_{\mathbf{w}})$
 $\left(\frac{\mathbf{c}_{\mathbf{f}}\mathbf{R}_{\mathbf{w}}}{\mathbf{N}_{\mathbf{w}}}\right)_{\mathbf{P}\mathbf{r}=1} = f(\mathbf{n}, \mathbf{S}_{\mathbf{w}})$
 $\left(\frac{\delta_{\mathbf{t}}\mathbf{r}}{\delta_{\mathbf{t}\mathbf{r}}}\right) = f(\mathbf{n}, \mathbf{S}_{\mathbf{w}})$

These functional relations are given in appendix B.

ues are given for the turbulent boundary layer at station 1, the program transfers to the If initial valroutine. If an initial value is given for the laminar boundary layer, the corresponding end of LAMNAR, where transformed quantities are computed for use by the TURBLN Initial values. - A check is made for initial values given by the user.

correlation number n_1 is computed, since the laminar equation is solved in terms of n. computed from the following relation obtained by rearranging equation (15), which is de-If a laminar momentum thickness is given, the corresponding correlation number n is rived in appendix A:

$$\frac{n_1}{4M_e} = \frac{-a_0' \theta_1^2}{\frac{\nu_0' (k_{Su})_1}{(k_{Su})_1}} \frac{1}{\left[1 + \frac{\gamma - 1}{2} \left(M_e^2\right)_1\right]}$$
(12)

If an initial laminar displacement thickness is given, the corresponding correlation num-ROOT, depending on whether the Mach number gradient $dM_{\rm e}/d(x/L)$ is positive or nega-Since $\delta^* = \theta H$ and θ and H are both functions of n, δ^* can be expressed as a ber is computed by calling the subroutine ROOT. Two calls are given in LAMNAR for Subroutine ROOT solves the following equation for n_1 , given δ_1^* : function of n.

$$\sum_{1}^{*} = \left\{ n_{1} \frac{-\nu_{0}'(k_{SU})_{L}}{a_{0}' \left[\frac{dM_{e}}{d\left(\frac{x}{L}\right)_{1}}\right]} \left[1 + \frac{\gamma - 1}{2} \left(M_{e}^{2}\right)_{1}^{-1} (3-\gamma)/(2\gamma - 2) \right\} \right\}$$

$$\times (-1.1138 \text{ n}_1 + 2.38411) \left[1 + (2.79 - 1.78 \text{ Pr}^{1/2}) \left\{ \left[1 + \left(s_{\text{w}} \right)_1 \right] \left[1 + \frac{\gamma - 1}{2} \left(M_{\text{e}}^2 \right)_1 \right] - 1 \right\} \right]$$

+
$$(4.65 \,\mathrm{Pr}^{1/3} - 3.65 \,\mathrm{Pr}^{1/2}) \left[\mathrm{Pr}^{1/2} \frac{\gamma - 1}{2} \left(\mathrm{M_e}^2\right)_1\right]$$
 (13)

This relation is obtained from equations (15) and (16).

If no initial laminar values are given, LAMNAR obtains n_1 in one of two ways. For a sharp leading edge, $n_1 = 0$. For stagnation point flow, n_1 is obtained from the curve against S_{W} . fit of n_{Sp}

lution to the laminar differential equation can be obtained. This solution is expressed in Solution of the laminar differential equation. - Using n₁ as an initial value, the soequation (4). Numerically, the solution is obtained from point to point by the following formula (see appendix A):

$${\rm (n)}_{\rm X_2/L} = \left[-{\rm AM_e^{-B}} \, \frac{{\rm dM_e}}{{\rm d} \left(\frac{\rm x}{\rm L} \right)} \left(1 + \frac{\gamma - 1}{2} \, {\rm M_e^2} \right) (3\gamma - 1)/(2\gamma - 2) \right]_{\rm X_2/L}$$

$$\times \begin{bmatrix} x_2/L & & & & \\ & M_e^{B-1} & & \\ & & & \\ & & & \\ x_1/L & & & \\$$

$$\begin{bmatrix} M_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ M_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{1}{M_{e}^{-B}} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 1)/(2\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right) (3\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{M_{e}}{2} M_{e}^{2}\right) (3\gamma - 2) \\ + \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{M_{e}}{2} M_{e}^{2$$

spacing represents a compromise between use of machine time and excessive accuracy in the solution of the equation. The resulting surface lengths and correlation numbers are A spacing of 1/500th of surface length L is used to step from point to point. This stored in tables. Calculation of laminar-boundary-layer parameters. Through interpolation, correlation numbers are obtained at the input-output stations on the boundary-layer surface. Using these values of n, the boundary-layer parameters are calculated.

Momentum thickness is obtained from the following equation (see appendix A):

$$\theta = \left\{ \frac{v_0' k_{su} L}{a_0'} \left[\frac{-n}{dM_e} \right] \left(1 + \frac{\gamma - 1}{2} M_e^2 \right)^{(3-\gamma)/(2\gamma - 2)} \right\}$$
(15)

Form factor is obtained from the following relation, obtained from reference 12:

$$H = (-1.1138 \text{ n} + 2.38411) \left\{ 1 + (2.79 - 1.78 \text{ Pr}^{1/2}) \left[(1 + S_{W}) \left(1 + \frac{\gamma - 1}{2} \text{ M}_{e}^{2} \right) - 1 \right] \right\}$$

+
$$(4.65 \,\mathrm{Pr}^{1/3} - 3.65 \,\mathrm{Pr}^{1/2}) \left(\mathrm{Pr}^{1/2} \,\frac{\gamma - 1}{2} \,\mathrm{M}_{\mathrm{e}}^{2}\right)$$
 (16)

Displacement thickness follows from

$$H\theta = *9$$

Adiabatic form factor is then obtained from the following equation (see appendix A):

$$H_{i} = \frac{H - Pr^{1/2} \frac{\gamma - 1}{2} M_{e}^{2}}{(1 + S_{w}) \left(1 + \frac{\gamma - 1}{2} M_{e}^{2} \right)}$$
(18)

5 is obtained from equation (41) of reference 4: Boundary-layer thickness

$$\delta = \theta \left\{ \left(\frac{\delta_{tr}}{\delta_{tr}} \right) + \frac{\gamma - 1}{2} M_e^2 \left[(1 + S_w) H_i + 1 \right] \right\}$$
 (19)

 S_{w} (see appendix B). The skin friction coefficient is then calculated from the follow-The shear-stress parameter l is obtained from the curve fit of l as a function of n ing equation (see appendix A): and

$$C_{f} = \frac{2l}{\sqrt{-\frac{1}{n} \frac{1}{M_{e}} \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \frac{x}{L}}}$$
(20)

Shear stress at the wall follows from

$$\tau_w = C_f \frac{1}{2} \rho_w u_e^2 \tag{21}$$

Laminar separation occurs when C_{f} or au_{w} attains a negative value.

The Reynolds analogy heat-transfer parameter $C_fR_w^{-}/Nu_X^{-}$ for Pr=1, is obtained from the curve fit of $C_fR_w^{-}/Nu_X^{-}$ as a function of n and S_w . The local Nusselt number is obtained from

$$l_{x} = \frac{C_{f} R_{w} P r^{0.3}}{\binom{C_{f} R_{w}}{N u_{x}}}$$
 (22)

which is a form of equation (38) of reference 4. The slope of the wall temperature profile is then calculated by using the definition of local Nusselt number

$$\mathbf{V}_{\mathbf{X}} = \frac{\mathbf{x} \left(\frac{\partial \mathbf{T}}{\partial \mathbf{y}} \right)_{\mathbf{W}}}{\mathbf{T}_{\mathbf{a}\mathbf{w}} - \mathbf{T}_{\mathbf{w}}}$$
(23)

and heat transfer per unit area is obtained from

$$q = k \left(\frac{\partial T}{\partial y} \right) \tag{24}$$

is obtained and compared with local incompressible as a function of momentum-thickness shape factor K (refs. 7 and 8). At each point in momentum-thickness Reynolds number $\left(R_{\theta}\right)_{i}$ (see fig. 8). When $\left(R_{\theta}\right)_{i}$ surpasses Check for instability and transition. - Position of instability is checked using Schlichting and Ulrich's curve of critical momentum-thickness Reynolds number the laminar boundary layer, $\left(\mathbf{R}_{ heta}
ight)_{ ext{cr}}$

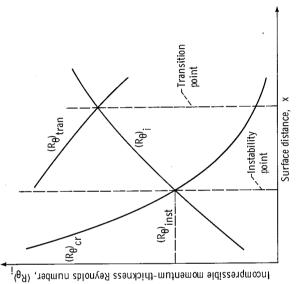


Figure 8. - Variation of variables used in prediction of transition.

 $\left(\mathbf{R}_{ heta}
ight)_{\mathrm{cr}}$, the boundary layer is assumed to be unstable. At each station after the point of instability, the mean pressure gradient parameter $\overline{\mathbf{K}}$ is computed from the following equation:

$$\overline{K} = \frac{1}{\frac{x}{L} - \left(\frac{x}{L}\right)_{inst}} \int_{x/L}^{x/L} K_{i} d\left(\frac{x}{L}\right)$$
(25)

Using Granville's results (ref. 9), the difference $\left(R_{\theta}\right)_{i,\Delta}$ between instability and transition momentum-thickness Reynolds numbers is obtained from a curve as a function of \overline{K} . This difference $\left(R_{\theta}\right)_{i,\Delta}$ is added to Reynolds number at instability $\left(R_{\theta}\right)_{inst}$ to obtain a local transition Reynolds number $\left(R_{\theta}\right)_{tran}$. Transition is assumed to occur when local incompressible Reynolds number $\left(R_{\theta}\right)_{i}$ attains a value larger than $\left(R_{\theta}\right)_{tran}$ (see fig. 8). Initial values for turbulent boundary layer. - After transition is located, initial valual. is added to Reynolds number at instability $\left(R_{ heta}
ight)$ inst

ues of f and H; are calculated for the solution of the turbulent-boundary-layer equa-

Subroutine TURBLN

Subroutine TURBLN solves the turbulent-boundary-layer equations, and computes the turbulent-boundary-layer parameters

transferred to TURBLN from LAMNAR. TURBLN calls RUNKUT, which uses these initial lent boundary layer. Once again a step size of 1/500th of the arc length L is used in the values for the solution of the coupled differential equations (eqs. (8) and (9)) of the turbusolution. The resulting distributions of f and H; are returned to TURBLN in tables. Solution of turbulent differential equations. - The initial values of f and H; are

values of f and H; are obtained at the input and output stations. By using these values Calculation of turbulent-boundary-layer parameters. - By means of interpolation, of f and $H_{\dot{1}}$, the boundary-layer parameters are calculated.

Transformed momentum thickness θ_{tr} is obtained by using the definition of the function f:

$$= \left(\frac{M_e a_0' \theta_{tr}}{\nu_0'}\right)^{1.268} \tag{26}$$

From transformed momentum thickness, actual momentum thickness is then calculated as follows:

$$\theta = \left(\frac{T_0}{T_e}\right)^{(\gamma+1)/(2\gamma-2)} \theta_{tr}$$
 (27)

The form factor is obtained from the incompressible form factor by the equation

$$H = H_{i}(1 + S_{w}) \left(1 + \frac{\gamma - 1}{2} M_{e}^{2} \right) + Pr^{1/3} \frac{\gamma - 1}{2} M_{e}^{2}$$
 (28)

Displacement thickness follows from

$$\delta \star = \theta H \tag{29}$$

p. 47). When the power law is used, the boundary-layer thickness δ can be obtained The power law is used for velocity profiles in the turbulent boundary layer (see from 5* through the relation

$$\delta = (1 + n_D)\delta * \tag{30}$$

The following relation is obtained from equation (10) of reference 5: The Ludwieg-Tillman skin friction relation, transformed for compressible flow, is used to obtain $C_{\mathbf{f}}$.

Shear stress at the wall follows from

$$\tau_{\rm W} = C_f \frac{1}{2} \rho_e u_e^2 \tag{32}$$

Heat transfer is obtained from C_{f} , as in reference 6,

$$q = \frac{C_f}{2} \frac{\rho_e u_e c_p}{P_r^{2/3}} (T_{aw} - T_w)$$
 (33)

The slope of the temperature profile at the wall $(\partial T/\partial y)_W$ is obtained from q/k, and the local Nusselt number is computed as defined:

$$Nu_{X} = \frac{x\left(\frac{\partial T}{\partial y}\right)_{W}}{T_{AW} - T_{W}}$$
(34)

Subroutine PROFIL

LAMNAR and TURBLN, and calculates and prints the laminar and turbulent velocity pro-Subroutine PROFIL prints all the principal boundary-layer parameters computed by

- Laminar profiles are computed using Pohlhausen's fourth-Laminar profiles. degree equation

$$\frac{\mathbf{u}}{\mathbf{u}} = \mathbf{a}\eta + \mathbf{b}\eta^2 + \mathbf{c}\eta^3 + \mathbf{d}\eta^4 \tag{35}$$

where

$$\eta = \frac{y}{\delta}$$

$$a = 2 + \frac{\lambda}{\delta}$$

$$b = -\frac{\lambda}{2}$$

$$c = -2 + \frac{\lambda}{2}$$

$$d = 1 - \frac{\lambda}{\delta}$$

and the shape factor

$$\lambda = \frac{\delta^2}{\nu_w} \frac{du_e}{dx}$$

- Turbulent profiles are computed using the power law Turbulent profiles.

$$rac{u}{u_{oldsymbol{
ho}}} = \left(rac{y}{\delta}
ight)^{1/n} \mathrm{p}$$

(36)

The power factor $\ensuremath{n_p}$ is obtained in TURBLN from the relation

$$H_{1} = \frac{2 + n_{p}}{n_{p}} \tag{37}$$

which follows from the definition of H_{i} and equation (36).

Subroutine RUNKUT

differential equations (8) and (9), are expressed as functions of x, f, $H_{\rm i}$, and some other H_1 are transferred from TURBLN. A step size Δx of $1/500 {
m th}$ of L is used. The two Subroutine RUNKUT solves the coupled ordinary differential equations of the turbulent boundary layer using a fourth-order Runge-Kutta method. Initial values of f and known quantities as follows:

$$\frac{\mathrm{df}}{\mathrm{dx}} = \mathbf{F}_1(\mathbf{x}, \ \mathbf{f}, \ \mathbf{H}_1) \tag{38}$$

$$\frac{dH_i}{dx} = F_2(x, f, H_i)$$

The following Runge-Kutta equations are then used from step to step

$$f_{N+1} = f_N + \frac{1}{6}(c_1 + 2c_2 + 2c_3 + c_4)$$
 (39)

$$\left(H_{i}\right)_{N+1} = \left(H_{i}\right)_{N} + \frac{1}{6}\left(d_{1} + 2d_{2} + 2d_{3} + d_{4}\right)$$
 (40)

where

$$c_{1} = \Delta x F_{1}(x_{N}, f_{N}, H_{i,N})$$

$$c_{2} = \Delta x F_{1}\left(x_{N} + \frac{\Delta x}{2}, f_{N} + \frac{c_{1}}{2}, H_{i,N} + \frac{d_{1}}{2}\right)$$

$$c_{3} = \Delta x F_{1}\left(x_{N} + \frac{\Delta x}{2}, f_{N} + \frac{c_{2}}{2}, H_{i,N} + \frac{d_{2}}{2}\right)$$

$$c_{4} = \Delta x F_{1}(x_{N} + \Delta x, f_{N} + c_{3}, H_{i,N} + d_{3})$$

(41)

and

$$d_{1} = \Delta x F_{2}(x_{N}, f_{N}, H_{i, N})$$

$$d_{2} = \Delta x F_{2}\left(x_{N} + \frac{\Delta x}{2}, f_{N} + \frac{c_{1}}{2}, H_{i, N} + \frac{d_{1}}{2}\right)$$

$$d_{3} = \Delta x F_{2}\left(x_{N} + \frac{\Delta x}{2}, f_{N} + \frac{c_{2}}{2}, H_{i, N} + \frac{d_{2}}{2}\right)$$

$$d_{4} = \Delta x F_{2}(x_{N} + \Delta x, f_{N} + c_{3}, H_{i, N} + d_{3})$$

$$(42)$$

Final tabulated values of f and H_i are returned to TURBLN.

Subroutine FUNCT

routine is called in order to obtain an initial correlation number corresponding to the dis-Since δ^* is a function of θ and H, and θ and H are both functions of correlation number n (see eqs. (15) and (16)), then 0* can be expressed as Subroutine FUNCT is called by the ROOT subroutine in LAMNAR when displacement a function of n. FUNCT expresses this functional relation of 0* and n for use by the thickness is given as an initial value for the laminar boundary layer. The ROOT subplacement thickness given. ROOT routine.

Function INT1

Function INT1 computes the integrand used in the first call on the SIMS1 integration The integral is the following:

$$\int_{\mathbf{x}_{+}/L}^{\mathbf{x}_{2}/L} \frac{\mathbf{M}_{\mathrm{e}}^{\mathrm{B}-1}}{\left(1+\frac{\gamma-1}{2}\,\mathrm{M}_{\mathrm{e}}^{2}\right)^{\!\!(3\gamma-1)/(2\gamma-2)}}\,\,\mathrm{d}\!\left(\!\frac{\mathrm{x}}{\mathrm{L}}\!\right)$$

which is part of equation (14).

Function INT2

Function INT2 computes the integrand used in the second call on the SIMPS1 integra-The integral is the following: tion routine.

$$\int_{(x/L)_{inst}}^{x/L} \kappa_i \, d \! \left(\! \frac{x}{L} \! \right)$$

which appears in equation (25).

DICTIONARY OF VARIABLES IN MAIN SUBROUTINES

combination of several terms in turbulent-boundary-layer equations

temporary variables in LAMNAR

A, A1, A2, A3, A4

coefficient in expression for Pohlhausen laminar velocity profiles AAA

based on T_e, ft/sec; speed of sound external to boundary layer a_e

m/sec

AΕ

value of Mach number M_e interpolated by LGRNGE in INT1 routine ANS

values of SW, ME, DMDL, DMDS, AA, BB, and TBAR interpolated ANS1, ANS2,

by LGRNGE calls in LAMNAR and RUNKUT routines ANS3, ANS4,

ANS5, ANS6

total distance along surface in x-direction, L, ft; m ARCL

speed of sound $a_0(a_0^{\dagger})$ based on static (total) temperature at sta-ASZ(ATZ)

tion 0, ft/sec; m/sec

temporary variable in LAMNAR and INT1

temporary variables in FUNCT B1, B2, B3, B4, B5 combination of several terms in turbulent-boundary-layer equations BB

coefficient in expression for Pohlhausen laminar velocity profiles BBB

coefficient in expression for Pohlhausen laminar velocity profiles CCC

array of coefficients for curve fit of $\,n_{\mbox{\footnotesize{\bf S}}\mbox{\footnotesize{\bf p}}}\,$ against $\,S_{\mbox{\footnotesize{\bf W}}}\,$ in LAMNAR CCN

array of coefficients for curve fit of $C_fR_W^{}/Nu_X^{}$ against n and $S_W^{}$ in LAMNAR CCRN

array of coefficients for curve fit of $\left({}^{\dag \mathcal{X}}_{U} \right)_{i,\;\Delta}$ against \overline{K} in LAMNAR array of coefficients for curve fit of $\,^{\circ}_{
m tr}/\,^{ heta}_{
m tr}\,$ against n and $m S_{
m w}$ in LAMNAR CDTH CDIF

skin friction coefficient at wall, $\,{
m C_{
m f}}$ CF

CFRW $C_f \sqrt{R_W}$

CMU

array of coefficients for curve fit of $\,\mu/\mu_{{\bf S}I}\,$ against $\,{
m T}/{
m T}_{{\bf S}I}\,$ PRECAL

correlation number, or pressure gradient parameter, n CORLN

CORLN/DMDL or $n / \left[dM_{e} / d(x/L) \right]$ CORML

specific heat at constant pressure, $c_{\rm p}$, (ft)(lbf)/(slug)($^{\rm O}$ R); J/(kg)(K) $_{
m CP}$

array of coefficients for curve fit of Pr against T/T $_{
m S}_l$ in PRECAL

array of coefficients for curve fit of $\left(\mathrm{R}_{ij}
ight)_{\mathbf{Cr}}$ against K in LAMNAR

CRCR

CRN

CPR

CSHR

Reynolds analogy parameter, $C_{
m f}R_{
m w}/{
m Nu}_{
m x}$

array of coefficients for curve fit of l against n and $S_{
m W}$ in

LAMNAR

table of correlation numbers (CORLN) obtained from CORML while solving laminar differential equation CTAB1

table of values of variable CORML computed by solving laminar differential equation CTAB2

array of coefficients for curve fit of $k/k_{\rm S}l$ against $T/T_{\rm S}l$ in PRECAL CTC

CTHET see INPUT

coefficient in expression for Fohlhausen laminar velocity profiles DDD

DEL small increment along x- or y-axis

displacement thickness, 5*, ft; m DELSR

full boundary-layer thickness, δ , ft; m DELTA

derivative of FX with respect to XX in FUNCT DFX

difference between transition and instability momentum-thickness DIFF

Reynolds numbers $\left(\mathrm{R}_{ heta}
ight)_{\mathbf{i},\,\Delta}$ in LAMNAR

DLAM see INPUT

 $DMDL \qquad \qquad dM_{\rm e}/[d(x/L)]$

 dM_{e}/dx , ft⁻¹; m⁻¹ DMDS

two-element array containing expressions for coupled ordinary dif-DOT

ferential equations for f and $H_{\hat{I}}$ in RUNKUT

slope of temperature profile at wall, $(\partial T/\partial y)_w$, $^0R/ft$; K/mDTDY

 $\delta_{\mathrm{tr}}/\theta_{\mathrm{tr}}$ in LAMNAR DTH

see INPUT DTURB du_e/dx , sec⁻¹

DUDS

logical variable indicating error in program due to improper input ERROR

ETA

 $\mathbf{f} = \left[(\mathbf{U}_e \theta_{tr})/(\nu_0') \right] \mathbf{1.268}$

polynomial function of $M_{\mbox{\scriptsize e}}$ and $S_{\mbox{\scriptsize w}}$ FF

form factor, H FORM adiabatic form factor, H_i FORMI initial value of H_i for turbulent boundary-layer equations FORMS

transformed form factor, $\mathbf{H_{tr}}$ FORMTR

initial value of f for turbulent boundary-layer equations FTRAN

value of function calculated in FUNCT

ratio of specific heats, γ GAM velocity head based on density external to boundary layer, $1/2\left(\rho_e u_e^2\right),~lbf/ft^2;~N/m^2$ HEADE

velocity head based on density at wall, 1/2 $(\rho_{\rm w}u_{\rm e}^2)$, lbf/ft²; N/m² heat transfer per unit area, (ft)(lbf)/(sec)(ft²); J/(sec)(m²) HEADW

HTRAN

integer iteration counter

integer location of station which ends boundary layer IEND

integer location of station at beginning (end) of laminar portion of IL1(IL2)

boundary layer

indicator of an infinite derivative (DFX) in FUNCT NF integer location of station where laminar instability occurs INST integer location of station where laminar or turbulent separation SEP

integer location of station at beginning (end) of turbulent portion of boundary layer IT1(IT2)

integer location of station where transition occurs from laminar to turbulent boundary layer

ITRAN

error indicator in call on SIMPS1

K1

see INPUT KATCH

mean shape factor based on momentum thickness, KBAR

integer counter indicating how many times input data has been KDONE

smoothed by calls on SMOOTH in PRECAL

see INPUT KEM

see INPUT KGRAD

see INPUT KLAM

see INPUT KLE

see INPUT KMAIN

see INPUT KPRE

see INPUT KPROF

see INPUT KPVM

see INPUT KSMTH KSDE

see INPUT

see INPUT KSPLN

integer iteration counter

Mach number external to boundary layer, M_e ME

dynamic viscosity based on reference temperature \overline{T} , $\overline{\mu}$, (lbf)(sec)/ft²; (N)(sec)/m² MUBAR

dynamic viscosity in English (metric) units at sea-level conditions, $\mu_{\rm Sl}$, (lbf)(sec)/ft²; (N)(sec)/m² MUSLE(MUSLM)

dynamic viscosity based on static (total) temperature at station 0, $\mu_0(\mu_0^*),~(lbf)(sec)/ft^2;~(N)(sec)/m^2$ MUSZ(MUTZ)

integer station number used in call on SIMPS1 in LAMNAR

see INPUT

NST

SN

NTAB

counter on STAB, CTAB, XTAB, and YTAB tables

see INPUT NTURB

 $\mathrm{Nu_{x}/\sqrt{R_{w}}}$ NURW

local Nusselt number, Nu_{x} NUSS kinematic viscosity based on static (total) temperature at station 0, NUSZ(NUTZ)

 $v_0(v_0^i)$, ft²/sec; m²/sec

kinematic viscosity at wall, $u_{
m w}$, ft $^2/{
m sec}$; m $^2/{
m sec}$

NUW

NV

number of coupled differential equations being solved by RUNKUT

routine - two in this program

see INPUT NVP

NVP + 1NVP1

see INPUT POPTZ reciprocal of power on power-law turbulent velocity profiles, POWER

Prandtl number, Pr

PR

see INPUT PRES

static pressure at station 0, P_0 , lbf/ft^2 ; N/m^2

see INPUT PTZ

PSZ

see INPUT ĸ critical incompressible momentum-thickness Reynolds number, RCRIT

 $\left(\mathrm{R}_{ heta}
ight)_{\mathrm{i,\,cr}}$

static density based on temperature external to boundary layer, $\rho_{\rm e},$ ${\rm slug/ft}^3;~{\rm kg/m}^3$ RHSE

static density based on wall temperature, $ho_{
m w}$, slug/ft 3 , kg/m 3 RHSW

static (total) density based on static (total) temperature at station 0, $\rho_0(\rho_0^*)$, slug/ft³; kg/m³ RHSZ(RHTZ)

incompressible momentum-thickness Reynolds number at instability RINS

point, $(R_{\theta})_{i, \, inst}$

momentum-thickness Reynolds number, \mathbf{R}_{θ} RTH

incompressible momentum-thickness Reynolds number, $\left(\mathbf{R}_{ heta}
ight)_{\mathbf{i}}$ RTHI

incompressible momentum-thickness Reynolds number used in check-RTRAN

ing for transition point, $\left(\mathbf{R}_{ heta}
ight)_{ ext{i, tran}}$

two-dimensional array of parameters used in Runge-Kutta scheme in RUNKUT RUK

Reynolds number at wall, $R_{\rm w} = u_{\rm e} x / \nu_{\rm w}$

RW

temporary values of independent and dependent variables in RUNKUT RX, RY

distance along surface from station 1, x, ft; m

S

second derivatives generated in call on SPLINE SDER

logical variable indicating whether separation has occurred SEPRN

dimensionless shape factor based on momentum thickness, SHAPK

Pohlhausen shape factor based on boundary-layer thickness, λ

SHAPL

shear parameter, l, in LAMNAR SHEAR

derivative of FUNCT in call on ROOT in LAMNAR

ratio of surface distance to total arc length, x/L

SOL

SL

limits of integration for calls on SIMPS1 in LAMNAR SOL1, SOL2

distance along surface from station 1, x

SS + DELSSDEL

table of surface distances x obtained in solving laminar differential STAB

equation

value of coefficient k_{Su} in Sutherland's viscosity temperature SUTHL

formula

temperature function at wall, $({\rm T_w/T_0^*})$ - 1 shear stress at wall, $_{\tau_w},~{\rm lbf/ft}^2,~{\rm N/m}^2$

TAUW

adiabatic wall temperature T_{aw} based on laminar recovery factor ${\rm Pr}^{1/2}, \, {}^{o}{\rm R}; \, {\rm K}$ TAWL

adiabatic wall temperature T_{aw} based on turbulent recovery factor TAWT

 $pr^{1/3}$, ^{0}R ; K

reference temperature, \overline{T} , ${}^{0}R$; K TBAR

thermal conductivity, k, $(ft)(lbf)/(ft)(sec)(^{O}R)$; J/(m)(sec)(K)

 $\mathbf{I}^{\mathbf{C}}$

temperature constant in Sutherland's temperature-viscosity formula TCON

thermal conductivity in English (metric) units at sea-level conditions, TCSLE(TCSLM)

 $k_{sl},~(\mathrm{ft})(\mathrm{lbf})/(\mathrm{ft})(\mathrm{sec})(^{O}R);~J/(m)(\mathrm{sec})(K)$

TEM, TEM1, temporary variables

TEM2, TEM3,

TEM4, TEM5,

TEM6, TEM7,

THET momentum thickness, θ , ft; m

 $heta_{
m tr}$ transformed momentum thickness, THETTR

TLAM see INPUT

TR1, TR2 temperature ratios in PRECAL

logical variable indicating whether transition has occurred TRANS

^oR; K static temperature external to boundary layer, $T_{\rm e}$, $_{
m LSE}$

total temperature in English (metric) units at sea-level conditions, TSLE(TSLM)

 T_{sl} , ^{0}R ; K

 $^{0}\mathrm{R};~\mathrm{K}$ static temperature at station 0, T_0 , ZSL

TTURB see INPUT

TTZ see INPUT

TWAL see INPUT

velocity within boundary layer, ft/sec; m/sec

UE see INPUT

þ

relative Mach number at station 0, M_0 UPMACH

UUE $u/u_{\dot{e}}$

relative velocity at station 0, u₀, ft/sec; m/sec Ω Z

VOVCR see INPUT

K see INPUT

ratio of X to maximum X-coordinate XOM obtained in solving turbulent differen-× table of surface distances XTAB

tial equations

distance along surface from station 1, X

Y see INPUT

dependent variable increments in Runge-Kutta scheme in RUNKUT YINC

ratio of Y to maximum X-coordinate YOM

distance normal to surface in y-direction in boundary-layer profile, computed by solving turbulent differential computed by solving turbulent differential ratio of YP to maximum X-coordinate table of values of H_i Ŧ table of values of equations equations YXMAX YTAB2 YTAB1 YP

dependent variables in solution of turbulent differential equations in RUNKUT

XX

AUXILIARY SUBROUTINES

The following general subroutines are called by the main subroutines, but do not use Each has its own variables, which are defined below instead of the COMMON variables. in the main dictionary.

Subroutine SMOOTH

 $_{\rm ot}$ > Subroutine SMOOTH is a simple data-smoothing routine. It smoothes an array by the following formula ¤ length

$$y_i = \frac{y_{i-1} + 2y_i + y_{i+1}}{4}$$
 $i = 2, n - 1$ (43)

If K = 1, the end points are also smoothed as follows:

$$y_1 = \frac{y_1 + 2y_2 - y_3}{2} \tag{44}$$

$$y_{n} = \frac{y_{n} + 2y_{n-1} - y_{n-2}}{2} \tag{45}$$

but this is not done in the BLAYER program.

The input variables for SMOOTH are as follows:

Y array y to be smoothed

- number of elements in array Y \mathbf{z}
- counter indicating whether end points are to be smoothed The output variable of SMOOTH is M
- array y after smoothing \succ

Subroutine GRADNT

Subroutine GRADNT computes the gradient of f(x) with respect to x using differ-

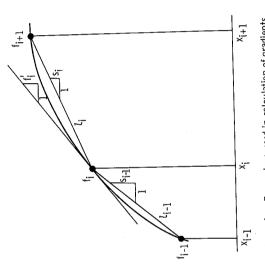


Figure 9, - Parameters used in calculation of gradients at input points.

ence techniques. Referring to figure 9, the slope of the function at any point $f_1'(x)$ is computed by weighting slopes between adjacent points

$$f_{i}^{1}(x) = \frac{S_{i}l_{i-1} + S_{i-1}l_{i}}{l_{i-1} + l_{i}}$$
 (46)

where

$$s_{i} = \frac{f_{i+1} - f_{i}}{x_{i+1} - x_{i}} \tag{47}$$

and

$$l_{i} = \sqrt{(f_{i+1} - f_{i})^{2} + (x_{i+1} - x_{i})^{2}}$$

(48)

Slopes at the end points are given by

$$f_1'(x) = s_1 + \frac{l_1}{l_1 + l_2} (s_1 - s_2)$$

(49)

$$f_n'(x) = s_{n-1} + \frac{l_{n-1}}{l_{n-1} + l_{n-2}} (s_{n-1} - s_{n-2})$$

(20)

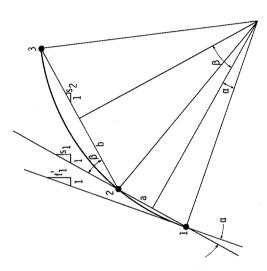


Figure 10. - Parameters used in calculation of gradients at end points.

Equations (49) and (50) can be derived from figure 10 where

 $\mathbf{f}_1' = \mathbf{s}_1 + \text{Change in slope due to angle } \alpha$

Assuming a circle

$$\frac{\alpha}{\beta} = \frac{\operatorname{arc} \ \alpha}{\operatorname{arc} \ \beta} \approx \frac{a}{a+b}$$

(51)

then,

Change in slope in
$$\alpha = \frac{a}{a+b}$$
 (Change in slope in β) = $\frac{a}{a+b}$ (s₁ - s₂) (52)

The input variables for GRADNT are as follows:

X independent variable, x

 $\mathbf{F}\mathbf{X} \qquad \mathbf{f}(\mathbf{x})$

N number of elements in array FX

The output variable of GRADNT is

DFDX gradient of f(x) with respect to x, f'(x)

Internal variables for GRADNT are as follows:

SL slopes between adjacent points, s

DIST distances between adjacent points, 1

Subroutine SPLINE

nomial function giving the spline fit curve. SPLINE uses the end condition that the second Subroutine SPLINE is based on the cubic spline curve. It solves the tridiagonal matrix equation given in reference 17 to obtain coefficients for the piecewise cubic polyderivative at either end point is equal to that at the adjacent spline point.

The input variables for SPLINE are as follows:

X array of x-coordinates

Y array of function values corresponding to X

N number of elements in X or Y array

The output variables of SPLINE are as follows:

at spline points array of first derivatives of Y with respect to X DYDX

array of second derivatives of Y with respect to X at spline points D2YDX2

Subroutine ROOT

values of f(x) are calculated by another subroutine FUNCT. ROOT divides the interval Subroutine ROOT locates a root for f(x) = y in the interval a, b (see fig. 11).

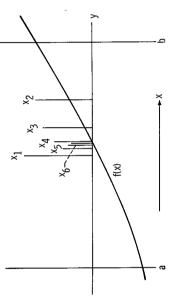


Figure 11. - Division of interval for location of a root.

It then divides that half and checks again. By repeating this procedure 20 times the root is located to within $1/(2^{20})$ of the a, b in half and checks which half contains the root. original interval.

ROOT contains an error message - ROOT HAS FALLED TO CONVERGE IN THE GIVEN INTERVAL - which is given if a root cannot be located within the tolerance This should never occur in the BLAYER program. (TOLERY) in 20 iterations.

The input variables for ROOT are as follows:

A a (see fig. 11)

B b (see fig. 11)

y (see fig. 11)

FUNCT external subroutine to calculate f(x)

|f(x) - y| < TOLERY)tolerance on solution (x is accepted if TOLERY

The output arguments for ROOT are as follows:

 \mathbf{X} value of \mathbf{x} such that $\mathbf{f}(\mathbf{x}) = \mathbf{y}$

derivative of f(x) with respect to x at the point f(x) = yDFX

Internal variables for ROOT are as follows:

left and right boundaries of interval in which root is located X1,X2

 $\mathbf{FX}, \mathbf{FX}1 \qquad \mathbf{f}(\mathbf{x})$

INF used to indicate infinite derivative, DFX

0 if finite

1 if infinite

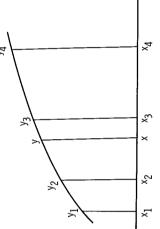


Figure 12. - Parameters used in Lagrangian interpolation.

Subroutine LGRNGE

Subroutine LGRNGE performs four-point interpolation using Lagrange's formula. Referring to figure 12, the formula is

$$y = f(x) = \frac{(x - x_2)(x - x_3)(x - x_4)}{(x_1 - x_2)(x_1 - x_3)(x_1 - x_4)} y_1 + \frac{(x - x_1)(x - x_3)(x - x_4)}{(x_2 - x_1)(x_2 - x_3)(x_2 - x_4)} y_2$$

$$+\frac{(x-x_1)(x-x_2)(x-x_4)}{(x_3-x_1)(x_3-x_2)(x_3-x_4)}y_3+\frac{(x-x_1)(x-x_2)(x-x_3)}{(x_4-x_1)(x_4-x_2)(x_4-x_3)}y_4$$
 (53)

The input variables for LGRNGE are as follows:

- X array of values of independent variable x
- array of values of dependent variable y
- N number of elements in X or Y array
- value of independent variable at which value of dependent variable is desired ARG

The output variable for LGRNGE is

value of dependent variable corresponding to ARG ANS

Subroutine CURVFT

The င် Subroutine CURVFT evaluates the polynomial f(x,y) using the coefficients general formula used is the following:

$$f(x,y) = C_1 \\ + C_{n+1}y \\ + C_{n+1}y \\ + C_{2n+1}y^2 \\ + C_{2n+1}y^2 \\ + C_{2n+1}y^2 \\ + C_{2n+2}xy^2 \\ + C_{2n+3}x^2y \\ + C_{2n+3}x^2y \\ + C_{2n+3}x^2y^2 \\ + C_{2n+3}x^{n-1}y^2 \\ + C_{2n+3}x^{n-1}y^2 \\ + C_{2n+1}y^{n-1} + C_{2n+2}xy^{n-1} + C_{2n+3}x^2y^{n-1} \\ + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1}y^{n-1} \\ + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1}y^{n-1} \\ + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1} + C_{2n+1}y^{n-1} \\ + C_{2n+1}y^{n-$$

This subroutine is also used for evaluating functions of one independent variable.

(54)

The input variables for CURVFT are as follows:

COEF array of polynomial coefficients, C_1 to C_{mn}

independent variable x

independent variable y

NX n - 1

NY m - 1

The output variable for CURVFT is

ANS dependent variable, f(x,y)

Function SIMPS1

A modification of Simpson's rule is used in which more intervals The interval speci-The local values of the fied by the limits of integration may be subdivided into as many as 200 subintervals in Function SIMPS1 performs numerical integration of a function of one variable beof smaller widths are placed in regions requiring greater accuracy. order to meet the criterion for accuracy built into the routine. tween specified limits.

In BLAYER, SIMP1 is used integrand are calculated by an external subroutine FUNC. twice, with functions INT1 and INT2 used for FUNC.

The input variables for SIMPS1 are as follows:

X1,X2 limits of integration

FUNC integrand, an external function

The output variables for SIMPS1 are as follows:

SIMPS1 value of the integral

error parameter set to 1 if SIMPS1 is unable to achieve a value of the integral which will pass its tests for accuracy KSIG

COMPLETE PROGRAM LISTING

SIBJOB SIBFIC BLAYER COMMON/C9/ERROR,TRANS,SEPRN LOGICAL ERROR,TRANS,SEPRN 20 5 20 63 TO 70 GO TO 10 10 IF (ERROR) GO TO IF (SEPRN) GO TO IF ("NOT-TRANS) G 60 TO IF(ERROR) GO TO (.NOT. TRANS) CALL LAMNAR CALL TURBLN CALL PROFIL CALL PRECAL IF (ERROR) (ERŔOZ) CALL INPUT 60 TO END 10 20

SIBFIC INPU

COMMON/C1/GAM.R.PTZ.TTZ.UPMACH.NST.NVP.NTURB.KPVM.KEM.KSMTH.
1K SPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE.KGRAD.KSDE.KLAM.
2K MAIN.KPR OF.X(100).Y(100).PRES(100).UE(100).ME(100).POPTZ(130).
3VOVCR(100).TWAL(130)
COMMON/C9/ERROR.TRANS.SEPRN LOGICAL ERROR, TRANS, SEPRN I SO CI FALSE. SUBROUTINE REAL ME TRANS= ERROR=

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070) NST, NVP, NTURB, TTURB
020) DLAM, TLAM, DTURB, TTURB
080) DLAM, TLAM, DTURB, TTURB
010) KPRE, KGRAD, KSDE, KLAM, KMAIN, KPROF
090) KPRE, KSRAD, KSDE, KLAM, KMAIN, KPROF
100, DR, NTURB, GT, NST, OR, KEM, LT, O, OR, KEM, GT, 1, OR, K ATCH, LT, O, OR, K ATCH, LT, O, OR, K ATCH, LT, O, OR, K ATCH
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1. 7x.5HKSPLN.8x.3HKLE.8x,5HKATCH.5x.5HCTHET/5x,13.8x,13.1
22.9x.12.10x.12.10x.12.10x.12.10x.12.10x.12.8x.F7.4)
1080 FORMAT( /6x.4HDLAM.7x.4HTLAM.8x.5HDTURB.7x,5HTTURB/4x,F10.10.6.2x.F10.6)
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WRITE(6,1120)
GO TO 60
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110.6.4x.F10.4))
1130 FORMAT(/9x.1Hx.11x.1HY.10x.5HPUPTZ.10x.4HTWAL/(3x.F10.5.2x.F10 5,2X,F10 .10X,4HTWAL/(3X,F10. IX.F10.6.4X.F10.41)
FORMAT(/9X.1HX.11X.1HY.10X.5HVOVCR END 1140 1110

SIBFIC PRECA

COMMON/C1/GAM,R,PTZ,TTZ,UPMAC4,NST,NVP,NTURB,KPVM,KEM,KSMFH,
1K SPLN,KLE,KATCH,CTHET,DLAM,TLAM,OTURB,TTURB,KPRE,KGRAD,KSDE,KLAM,
2K NAIN,KPRUF,X(100),Y(100),PRES(100),UE(100),ME(100),PUPTZ(130),
3VOVCR(100),TWAL(100) S COMMON/C3/XOM(100).YOM(100).S(100).SOL(100).AE(100).TSE(100). 1T AWL(100).TAWT(100).TBAR(100).RW(100).SW(100).SUTHL(100). 2R HSW(100).RH SE(100).HEADW(100).HEADE(100).NUW(100).WUBAR(100). 3A A(100).3B(100).FF(100).DUDS(100).DMDS(100).DMDL(100). COMMON/C2/PSZ.TSZ.UZ.ASZ.ATZ.RHSZ.RHTZ.MUSZ.MUTZ.NUSZ.NUTZ. DIMENSION SDER(100),CMU(20),CPR(20),CTC(20) REAL MUSZ,MUTZ,NUSZ,NUTZ,MUSLE,MUSLM,ME,NUW,MUBAR -.345113 ·--309112 ·--234136..1078624 DATA(CMU(I), I=1,5)/-.01945170,1.3019531, DATA(CTC(I), I=1,51/-, 03839323,1,2697427 CURVE FITS MUSLE= 3.711402E-7 MUSLM= 1.777029E-5 TCSLE= 3.202206E-3 TCSLM= 2.561796E-2 T SZ= TTZ/(1.+(GAM-1.)/2.*UPMACH**2) P SZ= P TZ* (T SZ/TTZ)**(GAM/(GAM-1.)) PARAMETER COMMON/C9/ERROR, TRANS, SEPRN AND TC DGICAL ERROR, TRANS, SEPRN TOTAL DATA(CPR(I), I=1,5)/.8557 1-.0236214,.00202863/ 1.068277826,-.00566593/ 1.08743781,-.009674725/ AND FOR MU. PR. PRECAL P SZ /R / TS Z /R/TT2 STATIC 518.688 288.160 SUBROUTINE 1PR. TC. ARCL INIT IAL 12E READ DATA =ZSH T SLM= HIZ

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| F(KPVM.EO.1) GO TO 70
| IF(KPVM.EO.2) GO TO 90
| IF(KPVM.EO.2) GO TO 10
| IF(KPVM.EO.4) GO TO 130
| IF(KPVM.EO.5) GO TO 150
| IF(KPVM.EO.5) GO TO 100
| IF(KPVM.EO.5) GO TO 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SORI((GAM+1.)/(GAM-1.)*(1.-PRES(I)/PTZ)**((GAM-1.)/GAM))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DQ 50 I=2,NST
XOM(I)= X(I)/X(NST)
YOM(I)= Y(I)/X(NST)
S(I)= S(I-1)+SORT((X(I)-X(I-1))**2+(Y(I)-Y(I-1))**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          EACH STATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALCULATE GEOMETRY RATIOS AND ARC LENGTHS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ΔI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CALCULATE PRES, UE, ME, POPTZ, AND YOVCR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALL CURVFT(CMU,MUSZ,TR1,0,4,0)
CALL CURVFT(CMU,MUTZ,TR2,0,4,0)
IF (KEN.EQ.1) GO TO 30
IC= TC*TCSLE
                                                                                                                                                                                                                                                                                         GO TO 20
TCON= 110.33
TRI= TSZ/TSLM
TR2= TTZ/TSLM
CALL CURVFT(CPR.PR.TR1.0.44.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CURVFI(CTC.TC.TR1.0.4.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       TSE(I)= TTZ-UE(I)**2/(2,*CP)
AE(I)= SORT(GAM*R*TSE(I))
ME(I)= UE(I)/AE(I)
POPTZ(I)= PRES(I)/PTZ
                                                                                                                                                  0
  SORT (GAM*R*TSZ)
                                   SORT (GAM*R*TTZ)
                                                                                                                                            IF (KEM.EQ.1) GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          XOM(1)= X(1)/X(NST)
YOM(1)= Y(1)/X(NST)
S(1)= 0.
                                                                                                         CP= R*GAM/(GAM-1.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MUSZ= MUSZ*MUSLM
MUTZ= MUTZ*MUSLM
NUSZ= MUSZ/RHSZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         I=1.NST
= S(I)/ARCL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MUSZ= MUSZ*MUSLE
MUTZ= MUTZ*MUSLE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           MUTZ/RHTZ
                                                                                                                                                                                TCDN= 198.60
TR1= TSZ/TSLE
TR2= TTZ/TSLE
                                                                       UZ= UPMACH#ASZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TC= TC*TC SLM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     S(NST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        P OP TZ ( I ) = VOVCR ( I ) =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GO TO 40
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SOL(1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             = 710 N
A SZ =
A TZ =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     09
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               80
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1-1.1)
POPIZ(I) = PRES(I)/PTZ
20 VOVCR(I) = SORT((GAM+1.)/(GAM-1.)*(1.-PRES(I)/PTZ)**((SAM-1.)/GAM))
GO TO 170
PRES SURE OVER TOTAL PRE SSURE GIVEN AS INPUT
I = 1.N ST
I = F(POPIZ(I) = LT. 0.. OR. POPIZ(I) . GT. 1.) GU TO 290
PRES(I) = POPIZ(I) **PTZ
UE(I) = POPIZ(I) **PTZ
UE(I) = SQRI(2.*GAM/(GAM-1.)*PTZ/RHIZ*(I.-(PRES(I)/PTZ)**((GAM-1.)/GAM))
T SE(I) = TIZ-UE(I) **2/(2.*CP)
AE(I) = SQRI(GAM*R*TSE(I))
AE(I) = UE(I) /AE(I)
AE(I) = UE(I) /AE(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               40 VOVCR(I) = SORT((GAM+1.)/(GAM-1.)*(1.-PRES(I)/PTZ)**((GAM-1.)/GAM))
GO TO 170
VELICITY OVER CRITICAL VELOCITY GIVEN AS INPUT
50 DO 160 I=1.NST
IF(VOVCR(I)-LT.0..OR.VOVCR(I).GT.SORT((GAM+1.)/(GAM-1.)))GO TO 290
PRES(I)= PTZ*(1.-((GAM-1.)/(GAM+1.)*VOVCR(I)**2)**(GAM-1.)))
UE(I)= SORT(2.*GAM/(GAM-1.)*PTZ/RHTZ*(1.-(PRES(I)/PTZ)**(GAM-1.))
                                                                                                                                                                                                                                                                                                                                                                                               GAM/ (GA4
                                                          Z*UE([] **2)/(2.*GAM*PTZ)) **( GAM/ (GA4
                                                                                                                                                                         POPTZ(I)= PRES(I)/PTZ
VOVCR(I)= SORT((GAM+1.)/(GAM-1.)*(1.-PRES(I)/PTZ)**((GAM-1.)/GAM)
IF(KDONE.GT.O) GO TO 190
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             .POPTZ(1), VOVCR(1), I=1, NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      WRITE(6.1000)
WRITE(6.1010) PSZ, TSZ, UZ, ASZ, A TZ, RHSZ, RHTZ, MUSZ, MUTZ, NUSZ, NJT
                                                                                                                                                                                                                                                                                       110 DO 120 I=1.N ST

IF(ME(I).LI.O.) GO TO 290

T SE(I)= TTZ/(I.+(GAM-1.)/2.*ME(I)**2)

AE(I)= SORT(GAM*R*TSE(I))

UE(I)= ME(I)*AE(I)

PRES(I)= PTZ*(I.-(GAM-1.)*RHIZ*UE(I)**2)/(2.*GAM*PTZ))**(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    STATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    EACH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    • ME ( I )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VOVCR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PRINT INITIAL CALCULATED PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   RITE(6,1020) (I,PRES(I),UE(I)
VELICITY GIVEN AS INPUT
90 DO 100 I=1.NST
IF(UE(I).LT.0.) GO TO 290
PRES(I)= PTZ*(1.-((GAM-1.)*RHI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       AND
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 TSE(I)= TT2-UE(I)**2/(2.*CP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF NECESSARY
                                                                                              I-1.))
T SE(I) = TTZ-UE(I) **2/(2.*CP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                AE(I)= SORT(GAM*R*TSE(I))
ME(I)= UE(I)/AE(I)
                                                                                                                                  AE(I)= SORT(GAM*R*TSE(I))
ME(I)= UE(I)/AE(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PRES, ME, POPTZ,
                                                                                                                                                                                                                                                                     AS INPUT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL SMOJTH(UE,NST.0)
KDONE=KDONE+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  POPTZ(1)= PRES(1)/PTZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INPUT DATA
                                                                                                                                                                                                                                                                        GI VEN
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                                                                                                                                                                                                                                                   GO TO 170
                                                                                                                                                                                                                                                                        MACH NUMBER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                SMOO TH
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AA(I)= BB(I)+TSE(I)/TBAR(I)+(MUBAR(I)/MUT2)+*.268
FF(I)=1.+.1750+ME(I)++2+.60+SW(I)+.4217+SW(I)+ME(I)++2+.3088+ME(I)
1++4+.0603+SW(I)+ME(I)++4+.1825+SW(I)+*2+.0735+SW(I)+*2*ME(I)+*2
                      WRITE(6,1020) (1,PRES(I),UE(I),ME(I),POPTZ(I),VOVCR(I),I=1,NST)
IF(KDONE,LI,KSMTH) GO TO 180
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WRITE(6.1060) (I.RW(I).SW(I).SUTHL(I).RHSW(I).RHSE(I).HEADM(I)
IHEADE(I).NUW(I).MUBAR(I).I=1.NST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        GD TD 260
(I.AE(I), TSE(I), TWAL(I), TAML(I), TAWT(I), TBAR(I)
                                                                                                                                     IF (KPRE.NE.1) GO TO 210
WRITE(6,1030) (1,x(1),Y(1),S(1),XGM(1),YGM(1),SOL(1),I=1,NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               BB(I)= ME(I)*ATZ/NUTZ*(TSE(I)/TTZ)**((GAM+1.)/(2.*GAM-2.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SURFACE
                                                                                                                                                                                                                                                                                                                                                                                                                                          NUW(I) = SUTHL(I)*NUTZ*(I,+SW(I))**2*TEM1**(GAM/(GAM-I,))
RW(I) = UE(I)*S(I)*NUW(I)
TAWL(I) = TSE(I)*(I,+PR**(I,/2,)*(TEM1-I,))
TAWL(I) = TSE(I)*(I,+PR**(I,/3,)*(TEM1-I,))
TAWL(I) = TSE(I)*(I,+PR**(I,/3,)*(TEM1-I,))
TAWL(I) = SF*(TWAL(I)+TSE(I))+*22*PR**(I,/3,)*(TTZ-TSE(I))
MUBAR(I) = MUTZ*SUTHL(I)*TBAR(I)/TTZ
                                                                                                                                                                                                                                                                                                                                                                                            SW(I)= TWAL(I)/TIZ-1.
SUTHL(I)= SORI(TWAL(I)/TIZ)*(TIZ+TCON)/(TWAL(I)+TCON)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     COMPUTE VELOCITY AND MACH NUMBER GRADIENTS ALONG THE
                                                                                                                                                                                                            CALCULATE OTHER NECESSARY PARAMETERS AT EACH STATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (I.DUDS(I).DMDS(I).DMDL(I).I=I.NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SPLINE CURVE TECHNIQUE
230 CALL SPLINE(S.UE.NST.DUDS.SDER)
CALL SPLINE(S.ME.NST.DMDS.SDER)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PRINT DIHER CALCULATED PARAMETERS
                                                                                                                                                                                                                                                                                                                                                  .5*R HSW(I)*UE(I)**2
.5*R HSE(I)*UE(I)**2
                                                                                                                                                                                                                                                                                 TEM1= 1.+.5*(GAM-1.)*ME(1)**2
                                                                                                                                                                                                                                                                                                   RHSW(I)= PRES(I)/R/TWAL(I)
RHSE(I)= PRES(I)/R/TSE(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL GRADNT(S, UE, NST, DUDS)
CALL GRADNT(S, ME, NST, DMDS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF(KGRAD.NE.1) GO TO 270
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        GO TO 230
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 2+ .0073*SW( [ ) ** 2 * ME ( [ ) * * 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TECHNIOUE
                                                                                        GEONETRY PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FOR IMPROPER INPUT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ARCL*DMDS(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  OI FFER ENCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       I F(K SPLN. EQ. 1)
                                                                                                                                                                                                                                                           I=1.NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      00 250 I=1,NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       I F ( K P R E . N E . 1 )
WRITE ( 6, 1050)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            WRITE(6,1060)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     WRITE(6.1080)
                    WRITE(6,1020)
 WRITE(6, 1040)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   MRITE(6.1070)
                                                                                                                                                                                                                                                                                                                                                   HEADW( I )=
                                                                                                                                                                                                                                                                                                                                                                        HEADE( I )=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             GO TO 240
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       220 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    240 DO 250 I=
250 DMDL(I)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11 =1.NST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FINITE
                                                                                        PRINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CHECK
190
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                                                                                                                                                                                                                                                                                                        , 3X, F9.5
                                                                                                                                                                                                                                                                                                                                                                                                      1050 FORMAT(///IX.7HSTATION,5X,2HAE,1OX,3HTSE,9X,4HTWAL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAWL,8X,4HTAW,4X,5HSW,4X,5HSW,4X,5HSW,4X,5HHEADE,9X,3HNUW,12X,5HWUBAR/(2X,13,3X,F15,1);
2X,F4,1,1X,F7,3,2X,614,6,2X,614,6,1X,F8,3,1X,F8,3,2X,614,5,2X,614,6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1070 FORMAT(IH1///21X.17HSURFACE GRADIENTS///)
1080 FORMAT(IX,7HSTATION,13X,4HDUDS,15X,4HDMDS,15X,4HDMDL/(2X,13,4X.Fl
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            OT HER
                                                                                                                                                                                                                          1020 FORMAT(/1X,7HSTATION,7X,4HPRES,13X,2HUE,12X,2HME,11X,5HPJPTZ,9X,5
1VOVCR/(2X,13,5X,F12,5,3X,F12,5,4X,F10,6,4X,F10,6,4X,F10,5))
1030 FORMAT(//1X,7HSTATION,7X,1HX,12X,1HY,12X,1HS,12X,3HXOM,9X,3HYOM,
                                                                                                                                                                            G15.7/5K, 10HARCL
                                                                                                                        G15.7/5x,10HMUTZ
G15.7//5x,10HCP
                                                                                                                                                                                                                                                                                                                                                          ME.
                                                                                                 F11.4//5X,10HRHSZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SI AL 104
                                                                                                                                                                                                                                                                                                                                                          • UE•
                                                                       F10.4/5X.10HUZ
                                                                                                                                                                                                                                                                                                     19X*3HSDL/(2X*I3*3X*F12.5*1X*F12.5*1X*F12.5.4X*F9.5.3X,F9.5
                                                                                                                                                                                                                                                                                                                                                          PRES
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                                                                                                                                                                                                                                                                                                                                                          DISTRIBUTIONS OF
                                                                                                                                                       Ħ
                                               CALCULATIONS///)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             A STAGNATION POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ITHAN STATION 1. THIS IS NOT ALLOWED)
1100 FORMAT(////10x,111HAN INPUT PRESSURE, VELOCITY
                                                                     F12.5/5x,10HTSZ =

F11.4/5x,10HATZ =

315.7//5x,10HMUSZ =

615.7/5x,10HNUTZ =

F9.5/5x,10HTC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          OR GREATER
                                                                                                                                                                                                                                                                                                                                                          1040 FORMAT(///1X,64HSMJOTHED SURFACE
                                                   1000 FORMAT(1H1///4X,24HPRELIMINARY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        1.6. IX. F18.6. IX. F18.6))
1090 FORMAT(/////10X.83HTHERE IS
                                                                                                       Ħ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            LESS THAN ZERO
                                                                                                                                                     615.7//5X,10HVUSZ
F11.4/5X,10HPR
F8.4///)
                                                                                                                              G15.7/5X.10HRHIZ
                                                                                                     1 F11-5//5X+10HASZ
                                                                            1010 FORMAT(5X+10HPSZ
                                                                                                                                                                                                                                                                                                                                                                                          1P TZ. AND VOVCR)
STATEMENTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF ITHER
   FORMAT
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10

9

DO 280 I=2,NST IF (UE(I).NE.O.)

270

WRITE(6.1090)

CONTINUE

280

RETURN ERROR=

WRITE(6.1100)

RETURN

.TRUE

290

LIBFTC LAMNA

AM, COMMON/C1/GAM.R.PTZ.TTZ.UPMACH.NST.NVP.NTURB.KPVM.KEM.KSMTH.
1K SPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE.KGRAD.KSDE.CL.
2K MAIN.KPROF.X(100).Y(100).PRES(100).UE(100).ME(100).PDPTZ(100). COMMON/C2/PSZ.TSZ.UZ.ASZ.ATZ.RHSZ.RHTZ.MUSZ.MUTZ.NUSZ.NJFL.CP L AMNAR SUBROUTIVE R. TC. ARCL

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              ITAWL(100). TAWT(100). TBAR(100). RW(100). SW(100). SUTHL(133).

2R HSW(100). RH SE (100). HEADW(100). HEADE(100). NUW(100). MUBAR(130).

3AA(100). BB(100). FF(100). DUDS(100). DMDS(103). DMDL(133).

COMMON/C4/THET(100). DELSR(100). DELTA(100). FORM(100).

IFORMI(100). FORMIR(100). RTH(100). RTHI(100). CF(100).
                                                                                                                                                                                         COMMON/C9/ERROR, TRANS, SEPRN
DIMENSION CORLN(100), CORML(100), SHEAR(100), DTH(100)
DIMENSION CON(20), CRCR(20), CDIF(20), CSHR(20), CCRN(20), CDIH(20)
DIMENSION STAB(505), CTABI(505), CTAB2(505)
REAL MUSZ, NUTZ, NUTZ, ME, NUM, MUBAR, NUSS, NURW, KBAR, INTI, INTELOGICAL ERROR, TRANS, SEPRN
        .AE(100), TSE(130)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   .ANJ. TLAM.GE.O. .AND.DTURB.GE.O. AND.TTURB.GE.D
                                                                                                                                                                                                                                                                                                                                                          AND DTH CURVE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       .97
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DATA(CCRN(I)+I=1,16)/2.02056,-19.7211,-24.0495,-1433.332
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 -256/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                DATA(CDIF(I).I=1,6)/903.785,26365.0,3.85695E+5,
11.11044E+6.-4.53853E+7,-7.70276E+7/
DATA(CSHX(I).I=1,16)/.224488,-1.91539,-9.894,-68.13488
1-.001512,-1.4768,-10.52925,-152.2781,-.002406,-.015629
1-1.45743,-126.23395,.000752,.005385,.917838,-39.40644/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1-.050979.-10.88012.62.4419.-5381.76.-.014343.2.279845.
1129.7008.-6257.848..0270567.-1.677051.57.4397.-2552.25.
DATA(CDIH(I).I=1.16)/8.02829.-4.30978.88.8244.36.4336.
12.71101.-7.42259.242.293.-16.293. -.16394.-7.61942.285
                                                                                                                                                                                                                                                                                                                                                         CRN.
  *SOL(100)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       .3276/
                                                                                                                                                                                                                                                                                                                                                                                                                                     .198
                                                                                                                                                                                                                                                                                                                                                                                                43
                                                                                                                                                                                                                                                                                                                                                        SHE AR.
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                                                                                                                                                                                                                                                                                                                                                                                                                             DATA(CRCR(I).1=1.61/5.47073,43.6053,227
1-2067.04.-27172.7.13691.2/
                                                                                                                                                                                                                                                                                                                                                                                                -.031
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   -3.70289,130,8107,111
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             10
                                                                                                                                  COMMON/C5/SHAPL(100),SHAPK(100),B.NS
COMMON/C6/FTRAN,FORMS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             09
  ,5(100)
                                                                                                                                                                                                                                                                                                                                                                                            05670,
                                                                                                                                                                                                                                                                                                                                                      DI FF,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 VALUES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         .AND. ITURB.GT.O.1
                                                                                                                                                                                                                                                                                                                                                                                         DATA (CCN( I) . I= 1,6)/-.08178..
  . YOM( 100)
                                                                                                                                                                                                                                                                                                                                                      RCRIT,
                                                                                                                                                                         COMMON/C7/IN ST.ITRAN.I SEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INITIAL
                                                                                                                                                                                                                                                                                                               FUNCT. INTL, INT2
                                                                                                                                                                                                                                                                                                                                                                                                               1.00873..01657.-.01052/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0
                                                                                                                                                                                                                                                                                                                                                     CORLN(1),
COMMON/C3/XOM(100)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      G
S
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       INITIALIZE PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CHECK CONSISTENCY OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  (NTURB.NE.1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         .GT.0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (DLAM.GE.0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           .TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WRITE(6, 1000)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       NUSS(1)= 0.
                                                                                                                                                                                                                                                                                                                                                   READ DATA FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          TAUM(1)= 0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               HTRAN( 1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    0
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                                                                                                                                                                                                                                                                                                             EXTERNAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DTOY(1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CRN(1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        R IRAN=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CF(1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ITRAN
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2. #3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (DMDL(1).GT.O.) CALL RODT(-1..O..DLAM.FUNCT..SE-5.CORLN(1).SL)
IF (DMDL(1).LT.O.) CALL RODT( O...2.DLAM.FUNCT..SE-5.CORLN(1).SL)
CORML(1) = CORLN(1)/DMDL(1)
                                                                                                                                                                                                                                                                                                                                                                                                                            TENI= 1.+.5*(GAM-1.)*ME(1)**2
FORM(1)= 2.38411*(1.+(2.79-1.78*PR**.5)*((1.+5W(1))*TEM1-1.))+(4.15*PR**(1./3.1-3.65*PR*.5)*PR**.5*(TEM1-1.)
THET(1)= DLAM/FORM(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             -A IZ*THET(1)**2/NUTZ/SUTHL(1)/ARCL/TEM1**((3.-GAM)/(
                                                                                                              FOR INITIAL VALUES
                                                                                                                                                                                                                                                      40 IF (TLAM.ED.O.) GD TD 50
INITIAL MOMENTUM THICKNESS WAS GIVEN
TEM1= 1.+.5*(GAM-1.)*ME(1)**2
CORML(1)= -ATZ*TLAM**2/NUTZ/SUTHL(1)/ARCL/TEM1**((3.-GAM)/...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            00 TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SURFACE
                                                                                                                 CHECK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          70 IF(KLE.NE.1.AND.ABS(DMDL(1)).3E..0001)
CORLN(1)= 0.
CORML(1)= 0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      THE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  80 CALL CURVFT(CCN+CORLN(1)+SW(1)+0+5+0)
                                                                                                                                                                                                                                                                                                                                                                              INITIAL DISPLACEMENT THICKNESS WAS GIVEN
                                                                                                                                                                     10
                                                                                                                                                                                                                                                                                                                                                                                              TO 50
                                                                                                                                                                    09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         NO IÑITIAL LAMINAR VALUES GIVEN
CALCULATE INITIAL CORRELATION NUMBER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CALCULATE CORRELATION NUMBERS ALONG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SOLVE LAMINAR DIFFERENTIAL EQUATION
                                                                                                                                   CORRELATION NUMBER
                                                                                                                  IN LAMINAR REGION
                                                                                                                                                                   If (DLAM.EQ.O.AND.TLAM.EQ.O.)
If (UE(1).GT.O.) 30 TO 40
ERROR = .TRUE.
WRITE(6,1030)
                                                                                                                                                                                                                                                                                                                                                                                              50 IF (ABSIDMDL(1)).GE..0001) GO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       TEM1= 1.+.5*(GAM-1.)*ME(1)**2
TEM2= (3.*GAM-1.)/(2.*GAM-2.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   60 TO 90
                                                                                                                                                                                                                                                                                                                                            CORLN(1) = CORML(1)*OMOL(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CORML(1)= CORLN(1)/DMDL(1)
                                 240
                                 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (CORML(1)-LT.0-)
                                 05
                 RETURN
IF (UE(1).GT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DEL = 0.002*ARCL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SHARP LEADING EDGE
                                                                                                                       BEGIN CALCULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   STAGNATION POINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      WRITE(6,1040)
                                                                                                                                    CALCULATE INITIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     .IRUE.
WRITE(6.1010)
                                                                  WRITE(6,1020)
                                                                                                                                                                                                                                                                                                                               1( 2.*GAM-2.1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CORML ( 1.)=
                                                                                                                                                                                                                                                                                                                                                                                                                    CORLN( 1)=
                                                                                                                                                                                                                                                                                                                                                                  90
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         GO TO 90
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 GO TO 90
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        14M-2-1)
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                                                    ERROR =
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                                                                                                                                                                                                                                                                                                                                                                   60 TO
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CALL LGRNGE(S, SW.NST, SS, ANS1)
CALL LGRNGE(S, ME, NST, SS, ANS1)
CALL LGRNGE(S, ME, NST, SS, ANS2)
CALL LGRNGE(S, ME, NST, SSDEL, ANS3)
CALL LGRNGE(S, DMDL, NST, SSDEL, ANS4)
A1= 0.43631-0.00367*ANS1+0.00681*ANS1**2+0.00651*ANS1**3
A2= 5.43220+2.25400*ANS1-0.06672*ANS1**2-0.20637*ANS1**3
A3= 4.51903-10.49775*ANS1-12.71732*ANS1**2-2.95270*ANS1**3
A4= 19.01831+62.76597*ANS1+115.00986*ANS1**2+62.53113*ANS1**3
A= A1-A3*CTAB1(NTAB)**2-2.**A4*CTAB1(NTAB)**3
B= A2+2.**A3*CTAB1(NTAB)*3.**A4*CTAB1(NTAB)**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   STATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CORLN AND
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   EACH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         F (CTAB1(NTAB).LT.-.32.0R.CTAB1(NTAB).GT..16)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LAYER PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALL LGRNGE(STAB.CTAB1.NTAB.S(I),CORLN(I))
CALL LGRNGE(STAB.CTAB2.NTAB.S(I).CORML(I))
FAIN SHEAR, CRN, AND DIH FROM CURVE FITS VS COICALL CURVETICSHR,SHEAR(I),CORLN(I),SW(I),3,3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ΑĪ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           13+31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (NTAB.GT.1) TEM4= ANS2**(-B)*TEM1**TEM2 TEM1= 1.4.5*(GAM-1.)*ANS3**2
TEM5= ANS3**(-B)*TEM1**TEM2
TEM6= -A*TEM5*TEM3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (NIAB.EQ.1) TEM7=0.

IF (NIAB.GI.1) TEM7= TEM5/TEM4*CTAB2(NTAB)

NIAB= NIAB+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      WRITE(6,1070) (STAB(I),CTAB1(I),I=1,NTAB)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 BOUNDARY LAYER PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CURVET(CCRN,CRN(I),CORLN(I),SW(I)
CURVET(CDTH, )TH(I),CORLN(I),SW(I)
                                                                                                                                                                                                                                                                                                                                                                                                        TO 110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     160
                                                                                                                                                                                                                                                                                                                                                                               TEM3 = SIMPSI(SOLI, SOL2, INTI, KI)
                                                                                                                                                                                                                                                                                                                                                                                                         09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CTABLICNTAB)= CTAB2(NTAB)*ANS4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               BOUNDARY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     09
                                                                                                                                                                                                                                                                                                                                                                                                   IF (TEM3.EQ.0..OR.K1.EQ.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 GO TO 100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (KSDE.NE.1) GD TO 130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GO TO 140
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (S(I).LE.STAB(NTAB))
OR - TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CTAB2(NTAB)= TEM6+TEM7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LAMINAR
                                     CORLN(1)
                                                                                                                                                                                                                                                                                                                                                               SS DEL /ARCL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        STABINTABLE SSDEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (SS.LT.ARCL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (KLAM.NE.1)
WRITE(6,1080)
                                                                                                            SSDEL = SS+DEL
                                                                                                                                                                                                                                                                                                                                              SS /ARCL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALCULATE LAMINAR
                                                                                                                                                                                                                                                                                                                                                                                                                       ERROR= .TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                           WRITE(6,1050)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     MRITE( 6, 1060)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(6,1090)
                                 CTAB1(1)= CC
CTAB2(1)= CO
STAB(1)= 0.
                                                                                          SS= SS+DEL
-DEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ERROR=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALCULATE
                                                                                                                                                                                                                                                                                                                                           SOL 1
SOL 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 OBTA IN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     130 IF
                                                                                           100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       140
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IF (I.EQ.1.AND.UE(1).EQ.O.) GG TO 190
SHAPK(I)= NUTZ*RTH(I)**2*SUTHL(I)**2*(1.+5W(I))**4/ATZ/ME(I)**2/
                         1(2.*GAM-2.)))
FORM(I) = (-1.1138*CORLN(I)+2.38411)*(1.+(2.79-1.78*PR**.5)*((1.+
1SW(I))*TEM1-1.))+(4.65*PR**(1./3.)-3.65*PR**.5)*PR**.5*(FEM1-1.)
DEL SR(I) = THET(I)*FORM(I)
RTH(I) = UE(I)*THET(I)/NUW(I)
FORMI(I) = (FORM(I)-SORT(PR)*(TEM1-1.))/((1.+SW(I))*TEM1)
SORT(-CORML(I)*NUIZ*SUTHL(I)*ARCL/AIZ*TEMI**([3.-GAM)/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SHAPK(I)= 0.07
RIHI(I)= RIH(I)*SJIHL(I)*(I.+SW(I))**2/FF(I)/SQRI(TEM1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALCULATE RCRIT TO CHECK FOR INSTABILITY AND TRANSITION
                                                                                                                                                        DELTA(1)= THET(1)*(DTH(1)+(TEM1-1.)*(FORMTR(1)+1.))
                                                                                                                                                                                                     IF (I.EO.1) GO TO 180
CFRW= 2.*SHEAR(I)*SORT(-SOL(I)/ME(I)/CORML(I))
                                                                                                                                                                                                                                                                                                                  DTDY(I)= NUSS(I)*(IAWL(I)-TWAL(I))/S(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CALL CURVFI(CRCR,RCRIT,SHAPK([).0.5.0)
RCRIT= EXP(RCRII)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1FF(1)/ARCL*DMDL(1)*TEM1**(1./(GAM-1.))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   TEM= SIMPSI(SOL(INST), SOL(I), INT2, K1)
IF (TEM.EG.O, OR.K1.EO.O) GO TO 220
                                                                                                                                                                         SHAPL(I)= DELTA(I) #*2/NUW(I) *0 UDS(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     0.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 KBAR= TEM/(SOL(I)-SOL(INST))
CALL CURVFT(CDIF,DIFF,KBAR,0,5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          270
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            27
                                                                                                                                      FORMTR(1) = FORMI(1)*(1.+SW(1))
                                                                                                                                                                                                                                                                                                                                                            GO TO 180
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IFIRTHIII .LI.RIRAN) GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF (I.L.T.NTURB) G3 T0 270
                                                                                                                                                                                                                                                                                                                                                                           GD TO 170
                                                                                                                                                                                                                                                                                              NUSS(I)= NURW#SORI(RW(I))
                                                                                                                                                                                                                                                                               NURW= CFRW*PR* . 3/CRN(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               I F( INST.NE.0) GD TD 210
                                                                                                                                                                                                                                       CF(I)= CFRW/SORI(RW(I))
TAUW(I)= CF(I)*HEADW(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF(RTHI(I).LT.RCRIT)
                                                                                                                                                                                                                                                                                                                                      HTRAN(I)= TC*DTDY(I)
IF (TAUW(I).GT.O.) GC
IF (KATCH.NE.O) GD TC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CHECK FOR INSTABILITY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CHECK FOR TRANSITION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         RIRAN= RINS+DIFF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  WRITE(6.1100)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            .TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                R INS= RTHI(I)
                                                                                                                                                                                                                                                                                                                                                                                                                    .TRUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                          11RAN= -2
GO TO 270
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GO TO 270
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GO TO 200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ERROR=
                                                                                                                                                                                                                                                                                                                                                                                                   SEP = I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                          RETURA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   INST=
                                                                                                                                                                                                                                                                                                                                                                                                                       SEPRN=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  K l = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    210
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            THE TURBULEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     1070 FORMAT(15(F12.5.2x,F7.4,3X1))
1080 FORMAT(1H1///1X,59HLAMINAR CALCULATION OF INSTABILITY AND TRANSITI
1081 LOCATIONS///1X,7HSTATION,2X,5HCORLN,5X,5HSHEAR,5X,3HDTH,6X,6HFO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GRADIENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GIVEN FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1030 FORMAT(////).10x,94HINITIAL VALUES OTHER THAN ZERO WERE GIVEN FOR ITHE LAMINAR BOUNDARY LAYER AT A STAGNATION POINT)
1040 FORMAT(////,10x,106HFOR THIS INPUT DATA STATION 1 IS ASSUMED TO 1E A STAGNATION POINT, SINCE NO INITIAL THICKNESSES ARE GIVEN, 210x,118HIN THIS CASE PRESSURE SHOULD DECREASE INITIALLY. EITHER
                                                                                                                                                                                                                                                                                                                                  FORMI(ITRAN) = (FORM(ITRAN)-PR**(1./3.)*(TEM1-1.))/((1.+S4(ITRAN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF(INST-EO.O .OR. INST-EO.I) WRITE(6,1120) I,CORLN(I),SHEAR(I),
1DTH(I).FORMTR(I).SHAPL(I).RTHI(I).SHAPK(I),RCRIT
IF(INST-NE.O .AND. INST.NE.I) WRITE(6,1130) I,CORLN(I),SHEAR(I),
1DTH(I).FORMTR(I).SHAPL(I).RTHI(I).KBAR,DIFF.RTRAN
IF (ITRAN-EO.-2) WRITE(6,1140)
IF(ITRAN-EO.-1.OR.ITRAN-EO.-2) GO TO 230
IF (I-EO.NST) RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  GIVEN FOR THE TURBULENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SOLUTION FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FOR DISPLACEMENT OR MOMENTUM THICKNESS,/
                                                                                                                                                                                                                                                                                                                                                                                          -GT-0.-AND-DIURB-EQ.O.-AND.IIURB-EQ.O.) THET(IIRAN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1050 FORMAT(////,10X,37HERROR IN COMPUTING INTEGRAL FOR CORLN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SHORT REGION OF FAVORABLE PRESSURE
                                                                                                                                                                                                                                                                                                                                                                                                                                            IHETIR= IHET(ITRAN)*(ISE(ITRAN)/ITZ)**((GAM+1.)/(2.*GAM-2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1010 FORMAT(////, 10x, 75HINITIAL VALUES WERE NOT GIVEN FOR
1T BOUNDARY LAYER AT STATION 1)
1020 FORMAT(////, 10x, 80HINITIAL VALUES WERE GIVEN FOR THE
1UNDARY LAYER AT A STAGNATION POINT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1000 FORMAT(////-10X,60HA NEGATIVE INITIAL VALUE HAS BEEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      .GT.O..AND.ITURB.GT.O.) FORMS=FORM! (ITRAN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1060 FORMATCIHI///7X.50HLAMINAR DIFFERENTIAL EQUATION -
                                                                                                             260
250
                            SOLUTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FTRAN= (ME(ITRAN) *AIZ*THETTR/NUTZ) **1.268
                                                                                                                                    10
                                                                                                                 <u>-</u>
                                                                                                             000
                            TURBUL ENT
                                                                                                                                                                                                                                                                                                     I EM 1= 1.+.5*(GAM-1.)*ME(IIRAN) **2
                                                                                                         IF (DTURB.EQ.O..AND.TTURB.EQ.O.)
IF (DTURB.GT.O..AND.TTURB.GT.O.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CORLN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF (RTRAN-LE.O.) RTRAN=1000.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              280
                                                                                                                                                                                                                                                                          FORM(ITRAN) = DIURB/ITURB
                          FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              60 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       BEGIN WITH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          VAL UE
                          VALUES
                                                                                                                                                                                                                                               THET(ITRAN)= ITURB
                                                                                                                                                                                                                                                                                                                                                                                                                 ICTHET*THET(ITRAN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 S NOT ALLOWED!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (KLAM.NE.1)
                                                                                                                                                                 ERROR = .TRUE.
WRITE(6.1110)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SIVE AN INITIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FORMAT STATEMENTS
                          COMPUTE INITIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IRLN///5124H
                                                                                                                                                                                                                                                                                                                                                                                          260 IF (CTHET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    IF (DTUR3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         41 0X • 60HDR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PRINT OUTPUT
                                                                                                                                                                                                                      RETURN
                                                                                                                                                                                                                                                                                                                                                               1* TEM 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2
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                                                                                240
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60 TO

80 踞 L•9x•4HR THI•6X•5HSHAPK•9X•5HRCRIT•6X•4HKBAR•13X•4HDI 0 THEY 2RMTR.4X.5HSHAPLL....

3FF.9X.5HRTRAN)

1090 FORMAT(/////10X.65HLAMINAR SOLUTION HAS PROCEEDED BETON.

1E WHERE IT IS VALID)

1100 FORMAT(/////10X.64HIF INITIAL TURBULENT VALUES ARE GIVEN, TH

1110 FORMAT(/////10X.64HIF INITIAL TURBULENT VALUES ARE GIVEN, TH

11H MUST BE NONZERD)

1120 FORMAT(f4.1X.5F10.4.1X.F12.1.1X.F12.1.)

1130 FORMAT(f4.1X.5F10.4.1X.F12.1.24X.F12.5.1X.F12.1.1X.F12.1.)

1140 FORMAT(/////10X.85HLAMINAR SEPARATION HAS OCCURRED, ASSUMED)

1 TRANSITION TO TURBULENT BOUNDARY LAYER) ASSUMED GIVEN.

SIBFIC TURBL

KLAM. SUBROUTINE TURBLN COMMOV/C1/GAM.R.PTZ.TTZ.UPMAC4.NST.NVP.NTURB.KPVM.KEM.KSMFH. 1KSPLN.KLE.KATCH.CTHET.DLAM.ILAM.DTURB.TTURB.KPRE,KGRAD.KSDE.KLA 2KMAIN.KPROF.X(100).Y(100).PRES(100).UE(100).ME(100).POPTZ(130). 3 IPR.TC.ARCL COMMON/C3/XGM(100), YGM(100), S(100), SGL(100), AE(100), TSE(130), ITAWL(100), TAWT(100), TBAR(100), RW(100), SW(130), SUTHL(133), 2R HSW(100), RH SE(100), HEADW(100), HEADE(100), NUW(100), MUBAR(130), 3AA(100), BB(100), FF(100), DUS(100), DMDS(103), DMDL(100), CGMMON/C4/THET(100), DELSR(100), DELTA(100), FGRM(100), IFORMI(100), FORMTR(100), RTH(100), RTHI(100), CF(100), COMMON/C6/FTRAN, F3RMS 3V NVCR(100), TWAL(100) COMMON/C2/PSZ, TSZ, UZ, ASZ, ATZ, RHSZ, RHTZ, MUSZ, MUTZ, NUSZ, NUTZ STAT ION = 1.+.5*(GAM-1.)*ME(I)**2 LGRNGE(XTAB.YTABI.NTAB.S(I).F) FR= NUTZ*F**.7886/ME(I)/AIZ [I)= THETTR*(TTZ/TSE(I))**((GAM+1.)/(2.*GAM-2.)) EACH BOUNDARY LAYER DIFFERENTIAL EQUATIONS IF (KSDE.NE.1) GD TO 10 WRITE(6,1000) WRITE(6,1010) (XTAB(1),YTAB1(1),YTAB2(1),1=1,NTAB) AB ΑT COMMON/C7/INST,ITRAN,ISEP COMMON/C8/XTA8(505),YTAB1(505),YTAB2(505),NT CALCULATE TURBULENT BOUNDARY LAYER PARAMETERS COMMON/C9/ERROR, TRANS, SEPRN REAL MUSZ.NUSZ.MUTZ.NUTZ.ME.NUW, MUBAR.NUSS 20 DO 30 I=ITRAN.NST IF (S(I).LE.XTAB(NTAB)) GO TO ISEP = I-1 = UE(I)*THET(I)/NUM(I) **ERROR, TRANS, SEPRN** SOLVE TURBULENT BUSING RUNGA-KUTTA .TRUE. CALL RUNKUT HET(1)= OGICAL S EPRN= RETURN T EM 1 00 0 20 ں پ پ ں ں ں

FORMTR(I) = FORMI(I) *(I) + SW(I))

FORMTR(I) = FORMI(I) + SW(I))

FORMI(I) = FORMI(I) + SW(I))

FORMI(I) = FORMI(I) - I.o.)

FOWER = 2.o./(FORMI(I) - I.o.)

IF (FTRMI(I) LT. 1.02) POWER = 100.

DELTA(I) = (1.+POWER) *DELSR(I)

CF(I) = 0.246*EXP(-1.561*FORMI(I)) *(UE(I) *THET(I) / NUTZ/(TEM1**(I.o.))

TAUW(I) = CF(I) *HEADE(I)

IF (I.E0.1) GO TO 30 HTRAN(I)= CF(I)/2./PR**(2./3.)*RHSE(I)*UE(I)*CP*(TAWT(I)-TAAL(I)) SOLUTION 111 FORMI **EQUATIONS** YTAB2,NTAB,S(I),FURMI(I)) DIFFERENTIAL ш DTDY(I)= HTRAN(I)/TC NUSS(I)= S(I)*DTDY(I)/(TAWT(I)-TWAL(I)) 1010 FORMAT((4(F10.5.2X.F8.1.2X.F7.4.2X))) FORMATI 1H1///5X + 62HTURBUL ENT CRN(I)= CF(I)*RH(I)/NUSS(I) FORMI ///4(31H =(1)SSNN ONA **CONTINUE** RETURN 1000 30

SIBFIC PROFI

SUBRDUTINE PROFIL COMMON/CI/GAM.R.PTZ.TTZ.UPMAC+.NST.NVP.NTURB.KPVM.KEM.KSMTH. 1K SPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE.KGRAD.KSDE.KLAM. 2< MAIN.KPROF.X(100).Y(100).PRES(100).UE(100).ME(100),PDPTZ(130), COMMON/C3/XOM(100). YOM(100). S(100). SOL(100). AE(100). TSE(100).

ITAML (100). TAWT(100). TBAR(100). RW(100). SW(100). SUTHL(100).

ZR HSW(100). RH SE(100). HEADW(100). HEADE(100). NUW(100). MUBAR(100).

3AA(100). BB(100). FF(100). DUDS(100). DMDS(100). DMDL(100).

COMMON/C4/THET(100). DELSR(100). DELTA(100). FORM(100).

IFORMI(100). FORMIR(100). RTH(100). RTHI(100). AND SEPARATION ITAUW(100), NU SS(100), DTDY(100), HTRAN(100), CRN(100) INSTABILLTY, TRANSITION, COMMON/C5/SHAPL(100), SHAPK(100), B, NS COMMON/C7/INST, ITRAN, ISEP 9 30 50 (KMAIN-NE-1) GO TO 10 3V DVCR(100) . TWAL (100) 60 ro GO TO WRITE(6.1030) ITRAN 09 #RITE(6,1010) INST PRINT LOCATIONS OF IF (ITRAN.LE.1) IF(ISEP.EG.O) WRITE(6.1050) WRITE(6,1000) IF(INST,E0.0) WRITE(6,1020) WRITE(6,1040) GO TO 20 40 60 TO 10 20 30 40

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WRITE(6.1140) (1.CF(1), TAUW(1), RT+(1), DTDY(1), NUSS(1), HFRAN(1)
                                                                                                                                                                                                                                                   WRITE(6.1120) (1.X(1).S(1).DELSR(1).THET(1).DELTA(1).FORM(1).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALCULATE AND PRINT LAMINAR BOUNDARY LAYER VELOCITY PROFILES
                            LAMINAR AND TURBULENT BOUNDARY LAYERS
                                                                                                                                 I TRAN, I END
                                                                                                                                                                                                             PRINT CALCULATED BOUNDARY LAYER PARAMETERS
                                                              .OR.IEND.EQ.O) IEND=ISEP
                                                                                                            CNET
                                                                                                                                                                                                                                                                                                                              COMPUTE BOUNDS ON VELOCITY PROFILES
                                                                                                WRITE(6,1070)
WRITE(6,1080)
WRITE(6,1090)
WRITE(6,1100)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                140
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1.-SHAPL(I)/6.
DELTA(I)/FLOAT(NVP)
                                                                                                                                                                                                                                        90
                                                                                                                                                                                                                                                                                                                                                                             TO 100
                                                                                                                                             G0 T0 80
                                                                                                                                                                             IF (KMAIN.NE.1) GD TD 90
WRITE(6,1100) ITRAN, IEND
                                                                                      GU TO 70
                                                                            (IEND.ED.O) IEND=NST
                                                                                                                                                                                                                                                                                                                                                     RETURN
                                                                                                                                                                    F(IEND.ED.O) IEND=NST
                                                                                                                                                                                                                                         G0 T0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                G0 T0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     -2.+.5* SHAPL(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            111=2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2.+5HAPL(I)/6
-.5*SHAPL(I)
                                                                                                                                                                                                                                                                                                                                                                             9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     N VP I= N VP + I
IF (IL 2 * L T • IL I) (
DO 130 I = IL I + IL 2
                                                                                                                                                                                                                                                                                                                                                      IF (KPRDF.NE.1) HARITE(6.1150)
IF(ITRAN.NE.0) G
                                                                                     (ITRAN.EG.1)
                                                                                                                                                                                                                                                                                                           ICRN(I), I=1, [END)
                                                                                                                                                                                                                                         (KMAIN.NE.1)
                                                                                                                                              F (ITRAN.LE.1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    WRITE(6,1160) I
                                PRINT LOCATIONS OF
                                                                                                                       ITRAN.E0.0)
                                                                                                                                  ( ITRAN.E0.1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     120 J=1.NVP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (III.E0.1)
                                                      ITRAN-1
                                                                ( IEND. ED.-1
                                                                                                                                                                                                                                                                                     WRITE(6.1130)
          WRITE(6,1060)
                                                                                                                                                                                                                                                                                                                                                                                                                                                         ITRAN-1
                                                                                                                                                        = ISEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ITRAN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                YP +DE1
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B BB=
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                                                      I END
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Y P=
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1150 FORMAT(1H1///1X,17HVELOCITY PROFILES///)
1160 FORMAT (/11X,7HSTATION,1X,15,2X,7HPROFILE/3X,7HY/DELTA,9K,
11140 FORMAT (/11X,7HSTATION,1X,15,2X,7HPROFILE,28X,2HN=,1X,F6.2/3X,7HY/D
1170 FORMAT (/11X,7HSTATION,1X,15,2X,7HPROFILE,28X,2HN=,1X,F6.2/3X,7HY/D
1ELTA,9X,1HY,12X,6HY/XMAX,10X,1HU,12X,4HU/UE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               *11X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    15 HDELTA,111X,4HFORM,10X,5HFORM!)
1120 FORMAT(2X,13,3X,2F13.6,F14.6,1X,F14.6,1X,F14.5,1X,2F14.4)
1130 FORMAT(///1X,7HSTATION,6X,2HC=,13X,4HTAUW,11X,3HRTH,14X,4HDFDY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (/10X+25HIRANSITION OCCURS AT STATION +13)
(/10X+30HSEPARATION OCCURS AT STATION +13)
(/10X+25HSEPARATION DOES NOT OCCUR)
(/10X+37HLAMINAR BOUNDARY LAYER DOES NOT OCCUR)
(/10X+42HLAMINAR BOUNDARY LAYER - STATIONS 1 TO +100X+42HLAMINAR BOUNDARY LAYER DOES NOT OCCUR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              1110 FORMATI/1X, 7HSTATION, 8X, 1HX, 12X, 1HS, 12X, 5HDELSR, 13X, 4HTHET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LAYER INFORMATION///
STATION .13)
                                                                                                                                     BOUNDARY LAYER VELOCITY PROFILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     STATIONS, 2X,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1140 FURMAT(15,F14.5,2X,F14.5,1X,F12.1,5X,F14.2,2X,F14.2,1X
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OCCUR)
STATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            OCCUR)
T STATION
                                 UUE= AAA#ETA+BBB#ETA*#2+CCC*ETA*#3+DDD*ETA**4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LAYER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1180 FORMAT(1X.F8.4.2X.2G15.6.2X.F9.2.6X.F8.4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          BOUNDARY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (/10X,31HINSTABILITY OCCURS AT (/10X,26HINSTABILITY DOES NOT (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (/10X+30HTRANSITION OCCURS AT (/10X+25HTRANSITION DOES NOT (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        BOUNDARY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  (/10x,39HTURBULENT BOUNDARY (/10x,35HTURBULENT BOUNDARY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             113X, 4HNUSS.10X, 5HHTRAN, 12X, 3HCRN)
                                                                                                                                                                                                                                                                                                                                                                                                                                               WRITE(6,1180) ETA, YP, YXMAX, U, UUE
                                                                               WRITE(6.1180) ETA.YP.YXMAX.U.UUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FORMAT ( 1H 1///1X, 36HPR I NCI PAL
                                                                                                                                            AND PRINT TURBULENT
                                                                                                                                                                                                                                DELTA (1) /DEL SR (1)-1
                                                                                                                                                                                                                                                                         DEL = DELTA(I)/FLOAT(NVP)
                                                                                                                                                                                                                                                     WRITE(6,1170) I.POWER
                                                                                                                                                                                                                                                                                                                                                                                                         UUE= ETA**(1./POWER)
                                                                                                                                                                                        RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               13///)
                                                                                                                                                                                                                                                                                                                                                             ETA= YP/DELTA(I)
                                                                                                                                                                                                                                                                                                                                                                                    YXMAX= YP/X(NST)
                                                                                                                                                                                                              00 160 I=IT1.IT2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1F14.4,2X,F13.3)
YP /DEL TA( I )
                    YXMAX= YP/X(NST)
                                                                                                                                                                                                                                                                                                                    On 150 J=1.NVP1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FORMAT STATEMENTS
                                                                                                                                                                                        IF( IT1.E0.0)
                                                                                                                                                                                                                                                                                                                                                                                                                               U = UUE * UE(I)
                                                               U = UUE * UE(I)
                                                                                                                                                                                                                                                                                                                                       YP= YP+DEL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                                                         CONTINUE
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                                                                                                                                               CALCULATE
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                                                                                                                                                                                                                                                                                                 ¥ P=
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S UBROUT INE

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COMMON/CI/GAM.R.PTZ.TTZ.UPMACH.NST.NVP.NTURB.KPVM.KEM.KSMFH.

1K SPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE.KGRAD.KSDE.KLAM.

2K MAIN.KPROF.X(100).Y(100).PRES(100).WE(100).ME(100).POPTZ(100).

3V GVCR(100).TWAL(100)

COMMON/C3/XOM(100).YOM(100).S(100).SUTHL(100).TSE(100).

2R HSW(100).TAWT(100).TBAR(100).HEADE(100).NUW(100).MUBAR(100).

3A A(100).BB(100).FF(100).DUDS(100).DMDS(100).DMDL(100).

COMMON/C6/FTRAN.FORMS

COMMON/C6/FTRAN.FORMS

COMMON/C6/FTRAN.FORMS

COMMON/C8/XTAB(505).YTAB1(505).YTAB2(505).NTAB

DIMENSION YY(2).RY(2).YINC(2).DOT(2).RUK(2,4)

DOUBLE PRECISION XX.RX.YY.RV.RY.RUK.DEL.DOT.

ITEM1.TEM2.TEM3.TEM4.TEM5.TEM6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     TEM1= 1.+(1.+ANS2)*YY(2)
TEM2= .123*EXP(-1.561*YY(2))*ANS3
DOT(1)= 1.268*(-YY(1)/ANS1*ANS5*TEM1+TEM2)
TEM3= YY(2)*(YY(2)+1.)**2*(YY(2)-1.)
TEM3= YY(2)*(YY(2)+1.)**2*(YY(2)-1.)
TEM4= 1.+ANS2*(YY(2)+YY(2)+4.*YY(2)-1.)/((YY(2)+1.)*(YY(2)+3.))
TEM4= (YY(2)*YY(2)-1.)*YY(2)/YY(1)*(.123*EXP(-1.561*YY(2))*ANS:
                          VALUE
                           INITIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INCREMENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 90 L=1,4

PUT DIFFERENTIAL EQUATIONS IN THE FORM OF
FIRST DEAIVATIVE = REMAINDER OF EQUATION
CALL LGRNGE(S,ME,NST,XX,ANSL)
CALL LGRNGE(S,SW,NST,XX,ANSL)
CALL LGRNGE(S,SW,NST,XX,ANSZ)
CALL LGRNGE(S,BB,NST,XX,ANSZ)
CALL LGRNGE(S,BB,NST,XX,ANSS)
CALL LGRNGE(S,DMDS,NST,XX,ANSS)
CALL LGRNGE(S,DMDS,NST,XX,ANSS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FORM OF
                           ORDER
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     NEXI
                                                                                                                                                                                                                                                                                                                                                                                                                                                SPACING AND STORE INITIAL
                        LEDUS FIRST
EQUATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     YY(2) AT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                AND YY (2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALCULATE NEW YY(1) AND YY(2
                    RUNKUT SOLVES SIMULTANEOUS
ORDINARY DIFFERENTIAL EQUAI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0.002*S(NST)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SOLVE FOR YY(1) AND
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SAVE PREVIOUS YY(1)
                                                                                                                                                                                                                                                                                                                                                                                                    ME.NUM. MUB
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Y TAB1(1)= YY(1)
Y TAB2(1)= YY(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    20 DO 30 J=1,NV
30 RY(J)= YY(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       YY(2)= FORMS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           XX= S(ITRAN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 YY( 1)=FTRAN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     X TAB(1)=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DEL=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  N V=2
                                                                                                                                                                                                                                                                                                                                                                                                                                                DEL
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/YY(1)*#(.7886)*(.011*(YY(2)+1.)*(YY(2)-1.)
                                                                                                                                                                                                              OBTAIN NEW YY(1) AND YY(2)
                                                                                                                                                                                                                                         **RUK(J.2)+2.*RUK(J.3)+RUK(J.4))/6
           1**2/YY(2) **2*TTZ/ANS6)*ANS4
DOT(2) = -ANS5*.5/ANS1*TEM3*TEM4+TEM5-TEM6
                                                                                                                                                                                                               10
                                                                                                                                                                                                                                                                                                 TABLE
                                                                                                                                                                                                                DEPENDENT VARIABLES
                                                                                                                                                                                                                                                                                                  4
                                                                                                                                                                                                                                                                                                                                                                                    20
                                                                                                                                                                                                                                                                                                   Z
                                                       DO 40 J=1,NV
O RUK(J.L) = DEL*DOT(J)
GO TO (50,50,70,90), L
O DO 60 J=1,NV
O Y(J)= RY(J)+RUK(J,L)/2.
                                                                                                                                                                                                                                                                      RE TURN
                                                                                                                                                                                                                                                                                                                                                                                   10
                                                                                                                                                                                                                                                                                                  STORE NEW COMPUTED VALUES
                                                                                                                                                                                                                                          YINC(3) = (RUK(3,1)+2
YY(3)= RY(3)+YINC(3)
                                                                                                                                           GO TO 90
DO 80 J=1,NV
YY(J)= RY(J)+RUK(J,L)
XX= RX+DEL
                                                                                                                                                                                                                                                                                                                                                                                    90
                                         APPLY THE RUNGA-KUTTA
                                                                                                                                                                                                                                                                                                                              NTAB = NTAB+1
YTAB1(NTAB)= YY(1)
YTAB2(NTAB)= YY(2)
                                                                                                                                                                                                                                                                     (YY(2).6T.2.8)
                                                                                                                                                                                                                                                                                                                                                                      X TAB(NTAB) = XX
IF (XX.LT.S(NST))
                                                                                                                                                                                                                               J=1.NV
                                                                                                                              XX= RX+DEL/2
                                                                                                                                                                                                        DO 100 JE?
                                                                                                                                                                                                   90 CONTINUE
                                                                                                                                                                                                                  INCR EMENT
                                                                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                                                                                                                                                           001
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SIBFTC FUNC

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SUBROUTINE FUNCT(XX,FX,DFX,INF)
COMMON/CI/GAM,R,PIZ,TIZ,UPMACH,NST,NVP,NTURB,KPVM,KEM,KSMTH,
1K SPLN,KLE,KATCH,CTHET,DLAM,TLAM,DTURB,TTURB,KPRE,KGRAD,KSDE,KLAM,
2K MAIN, KPROF,X(100),Y(100),PRES(100),UE(100),ME(100),POPTZ(100),
3VOVCR(100),TWAL(100)
COMMON/C2/PSZ,TSZ,UZ,ASZ,ATZ,RHSZ,RHTZ,MUSZ,MUTZ,NUSZ,NUTZ,CP,
                                                                                                                                                                                                                                                                                                                                                                                 = 0
1.+.5*(GAM-1.)*ME(1)**2
1.+(2.79-1.78*PR**.5)*([1.+SW(1))*B1-1.)
-NUTZ*SUTHL(1)*ARCL/ATZ/DMDL(1)*B1**((3.-GAM)/(2.*GAM-2.))
                                                                                                                                                                                                                         COMMON/C3/XGM(100), YGM(100), S(100), SOL(100), AE(100), TSE(100), 1T AWL(100), TAWT(100), TBAR(100), RW(100), SW(100), SUTHL(100), ZR HSW(100), RHSE(100), HEADW(100), HEADE(100), NUW(100), MUBAR(100), 3A A(100), BB(100), FF(100), DUD S(100), DMDS(100), DMDL(100) REAL MUSZ, NUSZ, MUTZ, NUTZ, ME, NUW, MUBAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            -1.1138*B2
2.38411*B2+(4.65*PR**(1./3.)-3.65*PR**.5)*PR**.5*(B1-1.(B3*XX)**.5*(B4*XX+B5)
(R3*XX)**.5*(B4*XX+B5)
(XX.E0.0.) GO TO 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (XX.EQ.O.) GO TO 10
= .5*[B3*XX]**(-.5)*B3*(B4*XX+B5)+B4*(B3*XX)**.
                                                                                                                                                                                                     1PR. TC. ARCL
                                                                                                                                                                                                                                                                                                                                                                                                                        81=
82=
83=
84=
85=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FX=
                                                                                                                                                                                                                                                                                                                                                                                                IN
```

RETURN 10 INF = 1 DFX = 1.E10 RETURN END

SIBFIC INTGI

COMMON/C1/GAM.R.PTZ.TTZ.UPMACH.NST.NVP.NTURB.KPVM.KEM.KSMTH.

IKSPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE.KGRAD.KSDE.KLAM.

ZKMAIN.KPRDF.X(100).Y(100).PRES(100).UE(100).ME(100).PDPTZ(100).

3VOVCR(100).TWAL(100)

COMMON/C3/XOM(100).YOM(100).S(100).SUTHL(100).TSE(100).

ITAWL(100).TAWT(100).YOM(100).HEADE(100).SW(100).MUBAR(100).

ZR HSW(100).RH SE(100).HEADW(100).HEADE(100).DMDL(100).MUBAR(100).

COMMON/C5/SHAPL(100).SHAPK(100).B.NS

COMMON/C5/SHAPL(100).SHAPK(100).B.NS

CALL LGRNGE(SOL.ME.NST.XX.ANS)

INTI= ANS**(B-1.)/((1.+.5*(GAM-1.)*ANS**2)** FUNC TION RETURN

SIBFTC INTG2

INT2= SHAPK(J-1)+(SHAPK(J)-SHAPK(J-1))*(XX-SOL(J-1))/(SOL(J)-SOL(J REAL FUNCTION INTE(XX)
COMMON/CI/GAM-R.PTZ.TTZ.UPMAC+.NST.NVP.NTURB.KPVM,KEM,KSMTH,
1K SPLN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE,KGRAD,KS)E.KLAM,
2K MAIN.KLE.KATCH.CTHET.DLAM.TLAM.DTURB.TTURB.KPRE,KGRAD,KS)E.KLAM,
2K MAIN.KPR OF.X(100).Y(100).PRES(100).WE(100).ME(100).PRES(100).
COMMON/C3/XOM(100).YGM(100).S(100).SQL(100).AE(100).TSE(100).
1TAWL(100).TAWT(100).YGM(100).HEADW(100).SW(100).SUTHL(100).
2R HSW(100).RHSE(100).HEADW(100).HEADE(100).NUW(100).MUBAR(100).
AAA(100).RHSE(100).FF(100).DUDS(100).DMDS(100).DMDL(100).
REAL ME.NUW.MUBAR.INT2
IF (NS.LT.4) GD TD 10 CALL LGRNGE(SOL, SHAPK, NS, XX, INT2) -LT-XX) GU TO 20 J=2.NS 00 20 J=2.N IF (SOL(J). CONTINUE RETURN 10 20

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SUBROUTINE SMOOTH(Y.N.K)

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Direction of the North Strategies of the North Strateg
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ×
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             WITH RESPECT
                                                  SIMPLE DATA SMOOTHING ROUTINE.
                                                                                                 END POINTS ARE ALSO SMOOTHED.
                                                                                                                                                                                     DIMENSION Y(100),Z(100)

N 1=N-1

DO 10 I=2,N1

O Z(I)= (Y(I-1)+2,*Y(I)+Y(I+1))/4,

Z(1)= Y(1)

Z(N)= Y(N)

IF(K,NE,1) GO TO 20

Z(1)=(Y(1)+2,*Y(2)-Y(3))/2,

Z(N)=(Y(N)+2,*Y(N)-Y(N-2))/2,

O DO 30 I=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GRADNT CALCULATES THE GRADIENT OF FX
USING FINITE DIFFERENCE TECHNIQUES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SUBROUTIVE GRADNT(X, FX, N, DFDX)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DIMENSION X(N).FX(N).DFDX(N)
DIMENSION SL(100).DIST(100)
                                        SMOOTH IS A
IF K=1, THE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SIBFIC GRADN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          20
                                                                                                                                                                                                                                                                                                                                               10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               20
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SIBFTC SPLIN

SUBROUTINE

AT THE SPLINE POINTS ADJACENT POINTS SPLINE FITS A SPLINE CURVE TO X AND Y AND CALCULATES FIRST AND SECOND DERIVATIVES END POINT SECOND DERIVATIVES EQUAL THOSE AT SPL INE(X,Y,N,DYDX,D2YDX2) 00000

```
1000 FURMATI////4X,49HRUOT HAS FAILED TO CONVERGE IN THE GIVEN INTERVAL
1/4X,3HA =,614.6,10X,3HB =,614.6,10X,3HY =,614.6)
                                                                                                                                                                                                                                                                                     40 DYDX(I)= (X(I)-X(I-1))/6.*(2.*D2YDX2(I)+D2YDX2(I-1))+(Y(I)-Y(I-1))
1/(X(I)-X(I-1))
                                                                                                                                                                                                                                      D2YDX2(K) = H(K1-G(K)*D2YDX2(K+1)
DYDX(1) = (X(1)-X(2))/6**(2.*D2YDX2(1)+D2YDX2(2))+(Y(2)-Y(1))/(X(2)
                                                                                          10 I=2.N1
(X(I)-X(I-1))/6.
(X(I+1)-X(I))/6.
2.*(A+B)-A*G(I-1)
(Y(I+1)-Y(I))/(X(I+1)-X(I))-(Y(I)-Y(I-1))/(X(I)-X(I-1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ROOT FOR (FUNCT-Y) IN THE INTERVAL (A.B)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SUBROUTINE RODT(A.B.Y.FUNCT.TOLERY.X.DFX)
X(N), Y(V), DYDX(N), D2YDX2(N)
G(100), 1(100)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF (ABS(Y-FX).LT.TOLERY) RETURN
WRITE(6,1000) A.B.Y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 09
                                                                                                                                                                   G(I)= B/C
H(I)= (D-A*H(I-1))/C
D2YDX2(N)= H(N1)/(1.+G(N1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DD 30 [=1.20

X = (X1+X2)/2.

CALL FUNCT(X,FX,DFX,INF)

IF ((FX1-Y)*(FX-Y).GI.0.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FUNCT(XI, FXI, DFX, INF
                                                                            20
                                                                              2
                                                                              .2) 60
                                                                                                                                                                                                                 DO 30 I=2.N
K= N+1-I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                4
     D IMENSION
D IMENSION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               GO TO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CONTINUE
                                  G(1) = -1.

H(1) = 0.
                                                                              IF (NI.LT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ROOT FINDS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             FX1= FX
                                                                N1= N-1
                                                                                                                                                                                                                                                                                                                                     RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                x 1= x
                                                                                                                                                                                                                                                                           1-x(1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                     SIBFIC ROD
                                                                                                           A = 0
                                                                                             00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             30
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SIBFTC LGRNG
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SUBROUTINE LGRNGE(X+Y+N+ARG,ANS)

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COE
                                                                                                                                                                                                                                                                                                                                                                                                                                            EVALUATE THE POLYNOMIAL FUNCTION, ANS=F(X,Y), USING COEFFICIENTS,
         LGRNGE PERFORMS 4 POINT LAGRANGIAN INTERPOLATION
                                                                                                                                                                                                                                                                                                                                                                                                                       SUBROUTINE CURVFT(COEF.ANS.X,Y.NX.NY)
                                 JENSION X(N).Y(N).XX(4).YY(4) (A3G-X(2)) 10,10,20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                                                                                                                                                                                                         ANS = C1*YY(1)+C2*YY(2)+C3*YY(
                                                                                                                                                                                                                                                                          1( xx(3) - xx(1) )/( xx(3) - xx(2) ) /
                                                                                                                                                                                                                                                                                     C4 = ((ARG-XX(1))*(ARG-XX(2))
I(XX(4)-XX(1))/(XX(4)-XX(2))/
                                                                                                                                                                                                                                                    1( xx(2)-xx(1) 1/(xx(2)-xx(3))
                                                                                                                                                                                                                     = ((ARG-XX(2))*(ARG-XX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             = ANS+COEF(K)*Y**(I-1)
                                                                         (ARG-X(N-1)) 40,40,30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               0.
                                                                                                                                 50,50,60
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = ANS+COEF(I)*X**(I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                .E0.
                                                                                                                                                                                                                            1(xx(1)-xx(2))/(xx(1))

C_2 = (ARG-xx(1))*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Ę
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COEF (20)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF (X-E0..0.AND.Y
IF (Y-E0..0) GD TI
IF (X-E0..0) GD TI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (I-1)*N×1+1
                                                                                                                                ( ARG-X(I))
                                                                                                                                                                                                (WWW)X
                                                                                                                                                                                                       = Y(MMM)
                                                                                                                   60 I=2.N1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COEF(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DO 40 I=2.NY1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 20 I=2,NX1
                                 D IMENSION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               = NX+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         NY+1
                                                               TO 70
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   D IMENSION
                                                                                       = N-3
                                                                                                 TO 70
                                                                                                                                                     TO 70
                                                                                                            I-N =
                                                                                                                                            = 1-2
                                                                                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               50
                                                                                                                                                                                                                                                                                                                    R ETURN
END
                                                                                                                                                                           00 80
                                                                                                                                                                                                                                                                                                                                                                                                   SIRFIC CURVE
                                                                                                                                                                                                           / / ( I )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             R ETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO
                                                                                                                                          ¥ 0
                                           # X O H X
                                                                                                 09
                                                                                                                       00
                                                                                                                                1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ANS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ANS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ANS
                                                                                                           <u>س</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        N Y 1
                                                                           20
                                                       10
                                                                                      30
                                                                                                           40
                                                                                                                                           20
                                                                                                                                                               90
                                                                                                                                                                                                            80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             40
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RETURN
50 ANS = .0
00 60 I=I.NYI
00 60 J=I.NXI
K = (I-1)*NXI+J
60 ANS = ANS+COEF(K)*Y**(I-I)*X**(J-I)
RETURN
PEND
```

SIBFTC SIMP

```
FUNCTION SIMPSI(X1.X2.FUNC.KSIG)
DIMENSION V(200).H(200).A(200).B(200).C(200).P(200).E(200)
LOGICAL SPILL
DOUBLE PRECISION ANS.D
DATA TWO.THREE.FOUR.THIRTY/2.0.3.0.4.0.30.0/
DATA T.NMAX.NSIG/3.0E-5.200.1/
INITIALIZE FIRST ELEMENTS OF ARRAYS.
                                                                                                                                                                                                                                                                                                                          TEST MAGNITUDE OF 4TH ORDER ERROR IN THIS INTERVAL-
IF (ABS(E(I)).LE.TEST) GO TO 30
IF (N.LT.NMAX) GO TO 20
GO TO FINISH IF STORAGE IS FILLED UP.
                                                                                                                                                                                                                                                                                                                                                                                                                                      4TH ORDER ERROR.
                                                                                                                                                                                                                                                                                                                                                                                                                                         AGAIN TO REDUCE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  H(N)=H(I)/TWO
A(N)=B(I)
B(N)=FUNC(V(N)+H(N))
C(N)=C(I)
P(N)=H(N)*(A(N)+FOUR*B(N)+C(N))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          p(I)=H(I)*(A(I)+F3UR*B(I)+C(I))
Q=P(I)+P(N)-Q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                B(I)=FUNC(V(I)+H(I))
                                                                                                                                                                                                                                                                         SPILL=-FALSE .
TEST=ABS(FRAC*ANS)
                                                                                                                                                                                                                                                                                                                                                                                                                                           INTERVAL
                                                                                                                                                                                             P =H* (A+FOUR*B+C)
                                                                                                                                                                                                                                                                                                                                                                                                 SPILL=.TRUE.
KSIG=KSIG+NSIG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (I)H+(I)A=(N)A
                                                                                                                                  H=(X2-V)/TWO
                                                                                                                                                                                                                                                                                                                      DO 30 I=1.K
                                                                                                                                              A =FUNC(V)
B=FUNC(V+H)
C=FUNC(X2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               C+SNA=SN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      HII)=H(N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 C(I)=4(N)
                                                                                                                                                                                                                                                                                                                                                                                                                              40
                                                                                                                                                                                                                                                                                                                                                                                                                                          SUBD IV IDE
                                                                                                                                                                                                                                                           FRAC=T
                                                                                                                                                                                                                                                                                                                                                                                                                                60 TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                              N=N+1
                                                                                                                                                                                                                             ANS=P
                                                                                                                                                                                                              ₽≡₽
                                                                                                                                                                                                                                             | | Z
                                                                                                                                                                                                                                                                                                                                                                                                                                                             20
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                                                                                                                                                                                                                                                                                                                                                                                                                                               ب
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E(I)=0 E(N)=0 30 CONTINUE TEST ALL INTERVALS AGAIN IF ANY WERE SUBDIVIDED THE LAST TIME. IF (N.GI.K) GD TD 10 ပ

L IEST ALL INTERVALS ASAIN IT AN IF (N-GI-K) GD TD 10 40 Q=0.0 DD 50 I=1.N 50 Q=0+E(I)

TIGHTEN ERROR LIMIT IF TOTAL ACCUMULATED ERROR TOO LARGE.

IF (ABS(0/T).LE.ABS(ANS).OR.SPILL) GO TO 60
FRAC=FRAC/TWO
GO TO 10 ں

GO TO 10
60 SIMPS1=(ANS+Q/THIRIY)/THREE
RETURN

Lewis Research Center,

National Aeronautics and Space Administration,

Cleveland, Ohio, January 8, 1970,

126 - 15.

A P P E N D I X A

DERIVATION OF EQUATIONS

DERIVATION OF EQUATION (14)

Equation (3) (which is eq. (32) of ref. 4) is the solution of equation (1), the laminar differential equation for correlation number n. When equation (3) is transformed to physical quantities, equation (33) of reference 4 results

$$\frac{n}{\frac{L}{u_e}} \frac{\frac{1-3\gamma}{2\gamma-2}}{\frac{T_0}{u_e}} \frac{\frac{1-3\gamma}{2\gamma-2}}{\frac{T_0}{u_e}} \frac{\frac{3\gamma-1}{2\gamma-2}}{\frac{T_0}{u_e}} \frac{\frac{3\gamma-1}{2\gamma-2}}{\frac{T_0}{u_e}} \frac{(\frac{T_0}{2\gamma-2})^{2\gamma-2}}{(\frac{T_0}{u_e})^{2\gamma-2}}$$
(A1)

Rearranging gives

$$n = -AM_e^{-B} \frac{T_0^i}{T_e} \frac{M_e}{u_e} \frac{du_e}{d(\frac{x}{L})} \left(\frac{T_0^i}{T_e}\right)^{2\gamma - 2} \frac{M_e^{B - 1}}{T_e} \frac{M_e^{B - 1}}{d(\frac{x}{L})} d(\frac{x}{L})$$
(A2)

By using the isentropic equations and the compressible Bernoulli equation, it is possible to obtain the relation

$$\frac{dM_e}{dx} = \frac{1}{a_e} \frac{T_0'}{T_e} \frac{du_e}{dx} \tag{A3}$$

When this substitution is made, equation (A2) becomes

$$n = -AM_e^{-B} \frac{dM_e}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_e^2\right)^{\frac{3\gamma - 1}{2\gamma - 2}} \begin{pmatrix} x \\ \frac{M_e^{-1}}{2} \end{pmatrix} \frac{M_e^{-1}}{\left(1 + \frac{\gamma - 1}{2}M_e^2\right)^{\frac{3\gamma - 1}{2}}} d\left(\frac{x}{L}\right)$$
(A4)

This agrees with equation (4).

In the program n is obtained at small incremental steps along the boundary-layer surface. Applying equation (A4) at any two adjacent steps yields

$${\rm (n)}_{\rm x_1/L} = \left[-{\rm AM_e^{-B}} \frac{{\rm dM_e}}{{\rm d}(\frac{\rm x}{\rm L})} \left(1 + \frac{\gamma - 1}{2} \, {\rm M_e^2} \right)^{\frac{3\gamma - 1}{2\gamma - 2}} \right] \\ = \left[-{\rm AM_e^{-B}} \frac{{\rm dM_e}}{{\rm d}(\frac{\rm x}{\rm L})} \left(1 + \frac{\gamma - 1}{2} \, {\rm M_e^2} \right)^{\frac{3\gamma - 1}{2\gamma - 2}} {\rm d}(\frac{\rm x}{\rm L}) \right]$$

$$= \left[-{\rm AM_e^{-B}} \frac{{\rm dM_e}}{{\rm d}(\frac{\rm x}{\rm L})} \right] \left(1 + \frac{\gamma - 1}{2} \, {\rm M_e^2} \right)^{\frac{3\gamma - 1}{2\gamma - 2}} {\rm d}(\frac{\rm x}{\rm L})$$

$$= \left(1 + \frac{\gamma - 1}{2} \, {\rm M_e^2} \right)^{\frac{3\gamma - 1}{2\gamma - 2}} {\rm d}(\frac{\rm x}{\rm L})$$

$$(n)_{x_2/L} = \begin{bmatrix} -AM_e^{-B} \frac{dM_e}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_e^2\right)^{\frac{3\gamma - 1}{2\gamma - 2}} \end{bmatrix}$$

$$J_{x_2/L} = \begin{bmatrix} -AM_e^{-B} \frac{dM_e}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_e^2\right)^{\frac{3\gamma - 1}{2\gamma - 2}} d\left(\frac{x}{L}\right) & (A6) \end{bmatrix}$$

But equation (A6) can be rewritten

$$(n)_{x_{2}/L} = \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2}} \end{bmatrix}$$

$$= \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2}} d\left(\frac{x}{L}\right) \end{bmatrix}$$

$$+ \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2}} d\left(\frac{x}{L}\right) \end{bmatrix}$$

$$+ \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2\gamma - 2}} d\left(\frac{x}{L}\right) \\ -\frac{3\gamma - 1}{2}M_{e}^{2} & \frac{3\gamma - 1}{2\gamma - 2} d\left(\frac{x}{L}\right) \end{bmatrix}$$

$$+ \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2\gamma - 2}} d\left(\frac{x}{L}\right) \\ -\frac{3\gamma - 1}{2}M_{e}^{2} & \frac{3\gamma - 1}{2\gamma - 2} d\left(\frac{x}{L}\right) \end{bmatrix}$$

$$+ \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2\gamma - 2}} d\left(\frac{x}{L}\right) \\ -\frac{3\gamma - 1}{2\gamma - 2} d\left(\frac{x}{L}\right) \end{bmatrix}$$

$$+ \begin{bmatrix} -AM_{e}^{-B} & \frac{dM_{e}}{d\left(\frac{x}{L}\right)} \left(1 + \frac{\gamma - 1}{2}M_{e}^{2}\right)^{\frac{3\gamma - 1}{2\gamma - 2}} d\left(\frac{x}{L}\right) \\ -\frac{3\gamma - 1}{2\gamma - 2} d\left(\frac{x}{L}\right) \end{bmatrix}$$

Then substituting for the first integral from equation (A5) gives

$$\begin{bmatrix} M_e^{-B} \frac{dM_e}{d(\frac{x}{L})} \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{2\gamma - 2} \\ M_e^{-B} \frac{dM_e}{d(\frac{x}{L})} \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{2\gamma - 2} \\ M_e^{-B} \frac{dM_e}{d(\frac{x}{L})} \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{2\gamma - 2} \\ - \begin{bmatrix} AM_e^{-B} \frac{dM_e}{d(\frac{x}{L})} \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{2\gamma - 2} \\ AM_e^{-B} \frac{dM_e}{d(\frac{x}{L})} \left(1 + \frac{\gamma - 1}{2} M_e^2\right)^{2\gamma - 2} \end{bmatrix} \end{bmatrix}$$

(14)

DERIVATION OF EQUATION (15)

Momentum thickness is calculated by equation (39) of reference 4:

$$\frac{\theta}{L} \sqrt{R_{W}} = \frac{T_{e}}{T_{w}} \sqrt{\frac{n^{\frac{X}{L}}}{L}}$$

$$-\frac{L}{u_{e}} \frac{du_{e}}{dx} \frac{T_{0}^{\dagger}}{T_{e}}$$
(A8)

Rearranging gives

$$\theta = \begin{pmatrix} -\frac{L}{2} \frac{x}{x} & \frac{u}{e} \frac{T_e^2}{T_w^2} & \frac{n}{T_e^2 du} \\ -\frac{L}{R_w} \frac{x}{L} & \frac{u}{L} \frac{T_e^2}{T_w^2} \frac{T_0'}{T_e'} \frac{du}{du} \end{pmatrix} = \begin{pmatrix} -L\nu_w & \frac{T_e^2}{T_w} & \frac{n}{T_e'} \\ -L\nu_w & \frac{T_e^2}{T_w} & \frac{T_0'}{T_e'} & \frac{du}{T_e'} \end{pmatrix}$$

Using equation (A3), this becomes

$$\theta = \left\langle \frac{L\nu_{\rm w}}{a_{\rm e}} \frac{T_{\rm e}^2}{T_{\rm w}^2} \left[\frac{-n}{dM_{\rm e}} \right] \right\rangle$$

(A9)

From the viscosity law of the form

$$\frac{\mu_{\rm w}}{\mu_0^{\prime}} = k_{\rm Su} \frac{T_{\rm w}}{T_0^{\prime}} \tag{A10}$$

it is easy to obtain the following relation:

$$\nu_{\rm w} = k_{\rm su} \nu_0^{\prime} \frac{T_{\rm w}}{T_0^{\prime}} \frac{\rho_0^{\prime}}{\rho_{\rm w}}$$
(A11)

Substituting equation (A11) into equation (A9) yields

$$\theta = \begin{cases} \frac{Lk_{Su}v_0^i}{a_e} \frac{\rho_0^i}{v_w} \frac{T_v^2}{T_w^2} \frac{-n}{dM_e} \\ \frac{a_e}{d\left(\frac{x}{L}\right)} \end{cases} = \begin{cases} \frac{Lk_{Su}v_0^i}{a_0^i} \left(\frac{T_0^i}{T_e}\right)^{1/2} \frac{P_0^i T_w}{P_w T_0^i} \frac{T_w}{T_0^i} \frac{P_0^i}{T_w^2} \frac{dM_e}{dM_e} \\ \frac{a_0^i}{d\left(\frac{x}{L}\right)} \end{cases}$$

Using $P_{w} = P_{e}$ and the isentropic relations results in

$$\theta = \left\{ \frac{L_{su} v_0'}{a_e'} \left(\frac{T_0'}{T_e} \right)^{\frac{3-\gamma}{2\gamma-2}} \left[\frac{1/2}{dM_e} \right]$$

$$\theta = \left\{ \frac{v_0' k_{su} L}{a_0'} \frac{-n}{dM_e} \left(1 + \frac{\gamma - 1}{2} M_e^2 \right)^{\frac{3-\gamma}{2\gamma-2}} \right\}$$

$$(15)$$

DERIVATION OF EQUATION (20)

Skin friction coefficient is calculated by equation (35) of reference 4:

$$C_{f}\sqrt{R_{W}} = 2l \sqrt{\frac{x}{L} \left(-\frac{L}{u_{e}} \frac{du_{e}}{dx}\right) \frac{T_{0}}{T_{e}}}$$
(A13)

Rearranging and using equation (A3), this becomes

$$C_f \sqrt{R_W} = 2l \left[-\frac{1}{n} \frac{1}{u_e} \frac{T_0}{T_e} \frac{T_e a_e}{T_0} \frac{dM_e}{d(\frac{x}{\tau})} \frac{x}{L} \right]^{1/2}$$

This equation reduces to

$$C_{\mathbf{f}} = \frac{2l \left[-\frac{1}{n} \frac{dM_{\mathbf{e}}}{M_{\mathbf{e}} \frac{x}{d\left(\frac{x}{\mathbf{L}}\right)} \frac{x}{L} \right]^{1/2}}{\sqrt{R_{\mathbf{w}}}}$$
(20)

DERIVATION OF EQUATIONS (18) AND (28)

equivalent incompressible form factor $H_{\hat{I}}$ for flows over insulated surfaces with In reference 18 the following expression is derived, relating form factor H

$$H = H_1 + \frac{\gamma - 1}{2} M_e^2(H_1 + 1)$$
 (A14)

For noninsulated surfaces, equation (A14) becomes

$$H = H_{tr} + \frac{\gamma - 1}{2} M_e^2 (H_{tr} + 1)$$
 (A15)

This is equation (40) of reference 4. Using the Crocco relation for a flat plate

$$\frac{h' - h_W}{h'_0 - h_W} = \frac{u}{u_e} = \frac{U}{U_e}$$
(A16)

it can be shown that

$$\int_0^{\delta_{tr} \left(\frac{h'}{h'_0} - 1\right) dY_{tr}} = \int_0^{\delta_{tr}} S dY_{tr} = S_w \theta_{tr} H_i$$
(A17)

Then the relation between the adiabatic and nonadiabatic transformed form factors

$$H_{tr} = \frac{\delta_{tr}^*}{\theta_{tr}} = \frac{\int_0^{\delta_{tr}} \left(1 - \frac{U}{U_e} + S\right) dY_{tr}}{\theta_{tr}} = H_1 + \frac{\int_0^{\delta_{tr}} S dY_{tr}}{\theta_{tr}}$$
(A18)

is used to obtain the relation

$$H_{tr} = H_1 + \frac{S_W \theta_{tr} H_1}{\theta_{tr}} = (1 + S_W) H_1$$
 (A19)

Substituting equation (A19) into equation (A15) gives

$$H = (1 + S_{w}) \left(1 + \frac{\gamma - 1}{2} M_{e}^{2} \right) H_{i} + \frac{\gamma - 1}{2} M_{e}^{2}$$
 (A20)

Solving for H_i results in

$$H_{i} = \frac{H - \frac{\gamma - 1}{2} M_{e}^{2}}{(1 + S_{w}) \left(1 + \frac{\gamma - 1}{2} M_{e}^{2}\right)}$$
(A21)

For nonunity Prandtl number and laminar flow, equation (A21) becomes

$$H_{i} = \frac{H - Pr^{1/2} \frac{\gamma - 1}{2} M_{e}^{2}}{(1 + S_{w}) \left(1 + \frac{\gamma - 1}{2} M_{e}^{2} \right)}$$
(18)

$$H_1 = \frac{H - Pr^{1/3} \frac{\gamma - 1}{2} M_e^2}{(1 + S_w) (1 + \gamma - 1 M_z^2)}$$

(28)

APPENDIX B

CURVE FITS USED IN PROGRAM

Coefficients for the curve fits are read in at the beginning of each of these routines, and values are Polynomial curve fits are used in the PRECAL and LAMNAR routines. calculated by means of calls on the CURVFT routine.

In PRECAL the following curve fits are used:

(1) Nondimensional dynamic viscosity of air as a function of nondimensional static temperature, $\mu/\mu_{Sl} = f(T/T_{Sl})$:

$$\frac{\mu}{\mu_{Sl}} = -0.0194517 + 1.3019531 \left(\frac{T}{T_{Sl}}\right) - 0.34511323 \left(\frac{T}{T_{Sl}}\right)^2$$

+ 0.068277826
$$\left(\frac{T}{T_{sl}}\right)^3$$
 - 0.00566593 $\left(\frac{T}{T_{sl}}\right)^4$ (B1)

CMU is used for the storage of these coefficients. The following values are used for the sea-level reference conditions $T_{\mathbf{S}l}$ and $\mu_{\mathbf{S}l}$:

$$T_{sl} = 518.688^{0} R = 288.160 K$$

$$\mu_{\rm Sl} = 0.3711402 \times 10^{-6} \frac{({\rm lbf})({\rm sec})}{{\rm ft}^2} = 0.1777029 \times 10^{-4} \frac{({\rm N})({\rm sec})}{{\rm m}^2}$$

(2) Prandtl number of air as a function of nondimensional static temperature,

$$Pr = 0.85570 - 0.234136 \left(\frac{T}{T_{Sl}}\right) + 0.1078624 \left(\frac{T}{T_{Sl}}\right)^{2}$$

(B2)

 $0.0236214 \binom{\mathrm{T}}{\mathrm{T}_{Sl}} + 0.00202863 \binom{\mathrm{T}}{\mathrm{T}_{Sl}}$

CPR is used for the storage of these coefficients.

(3) Nondimensional thermal conductivity of air as a function of nondimensional static temperature, $(k/k_{Sl}) = f(T/T_{Sl})$:

$$\frac{k}{k_{Sl}} = -0.03839323 + 1.2697427 \left(\frac{T}{T_{Sl}}\right) - 0.30911252 \left(\frac{T}{T_{Sl}}\right)^2$$

+ 1.08743781
$$\left(\frac{T}{T_{Sl}}\right)^3$$
 - 0.009674725 $\left(\frac{T}{T_{Sl}}\right)^4$ (B3)

CTC is used for the storage of these coefficients. The following values are used for ${
m k_{f S}l}$

$$k_{Sl} = 0.3202206 \times 10^{-2} \frac{(ft)(lbf)}{(ft)(sec)(^{O}R)} = 2.561796 \times 10^{-2} \frac{J}{(m)(sec)(K)}$$

In LAMNAR the following curve fits are used:

(1) Stagnation point correlation number against wall temperature function, $n_{sp} = f(S_w)$:

$$n_{sp} = -0.08178 + 0.06670 S_{w} - 0.03143 S_{w}^{2} + 0.00873 S_{w}^{3}$$

+ 0.01657
$$S_{W}^{4}$$
 - 0.01052 S_{W}^{5} (B4)

CCN is used for the storage of these coefficients. This is an expression for the "twodimensional body" curve in figure 6 of reference 4.

(2) Critical momentum-thickness Reynolds number against shape factor based on momentum thickness, $\left(R_{\theta}\right)_{cr}=f(K)$:

$$\left(\mathbf{R}_{\theta}\right)_{c,r} = \exp(5.47073 + 43.6053 \text{ K} + 227.198 \text{ K}^2 - 2067.04 \text{ K}^3$$

CRCR is used for the storage of these coefficients. This curve is plotted as figure 3 of reference 9.

(B₂)

 $-27172.7 \,\mathrm{K}^4 + 13691.2 \,\mathrm{K}^5$

(3) Difference between instability and transition momentum-thickness Reynolds numbers against mean shape factor based on momentum thickness, $\left(R_{\theta}\right)_{i,\Delta} = f\left(\overline{K}\right)$:

$$\left(\mathbf{R}_{\theta}\right)_{\mathbf{i},\;\Delta} = 903.785 + 26.365.0\ \overline{\mathrm{K}} + 385.695.0\ \overline{\mathrm{K}}^2 + 1.110.440.0\ \overline{\mathrm{K}}^3$$

- 45 385 300.0
$$\overline{K}^4$$
 - 77 027 600.0 \overline{K}^5 (B6)

CDIF is used for the storage of these coefficients. This curve is plotted as figure 4 of reference 9.

(4) Shear parameter against correlation number and wall temperature function, $= f(n, S_w)$:

$$t = 0.224488 - 1.91539 n - 9.89400 n^2 - 68.13488 n^3 - 0.001512 S_{w}$$

$$-1.47680 S_{\rm w}^{\rm n} - 10.52925 S_{\rm w}^{\rm n}^2 - 152.2781 S_{\rm w}^{\rm n}^3 - 0.002406 S_{\rm w}^2$$

$$-0.015629 S_{\rm w}^2 {\rm n} - 1.45743 S_{\rm w}^2 {\rm n}^2 - 126.23395 S_{\rm w}^2 {\rm n}^3 + 0.000752 S_{\rm w}^3$$

$$+0.005385 S_{\rm w}^3 {\rm n} + 0.917838 S_{\rm w}^3 {\rm n}^2 - 39.40644 S_{\rm w}^3 {\rm n}^3$$
(B7)

 $S_{\rm w}$ = -0.8 and -1.0, as well as the reversal on the $S_{\rm w}$ = 1.0 curve, are not reflected in CSHR is used for the storage of these coefficients. This is a representation of the curves of figure 2 in reference 4. The double-valued portions of the curves for equation (B7).

(5) Reynolds analogy parameter against correlation number and wall temperature function, $C_f R_W / N u_X = f(n, S_W)$:

$$\frac{C_f R_w}{N u_x} = 2.02056 - 19.7211 \, n - 24.0495 \, n^2 - 1400.002 \, n^3 - 0.050979 \, S_w$$

$$-10.88012 \, S_{w}^{}n + 62.4419 \, S_{w}^{}n^{2} - 5081.76 \, S_{w}^{}n^{3} - 0.014343 \, S_{w}^{2} \\ + 2.279845 \, S_{w}^{}n + 129.7008 \, S_{w}^{}n^{2} - 6257.848 \, S_{w}^{}n^{3} + 0.0270567 \, S_{w}^{}3 \\ -1.677051 \, S_{w}^{}n + 57.4397 \, S_{w}^{}n^{2} - 2552.266 \, S_{w}^{}n^{3}$$
 (B8)

 $S_{\rm W} = 1.0,$ This is a representation of the curves in figure 3 of reference 4. The double-valued regions at the ends of the -0.8, and -1.0 curves are not reflected in equation (B8). CCRN is used for the storage of these coefficients.

(6) Thickness ratio parameter against correlation number and wall temperature function, $\delta_{tr}/\theta_{tr} = f(n, S_{w})$:

$$\frac{\delta_{tr}}{\theta_{tr}} = 8.02829 - 4.30978 \text{ n} + 88.8244 \text{ n}^2 + 36.4336 \text{ n}^3 + 2.71101 \text{ S}_{w}$$

$$- 7.42259 \text{ S}_{w} \text{ n} + 242.293 \text{ S}_{w} \text{ n}^2 - 16.293 \text{ S}_{w} \text{ n}^3 - 0.16394 \text{ S}_{w}^2$$

$$- 7.61942 \text{ S}_{w}^2 \text{ n} + 286.9795 \text{ S}_{w}^2 \text{ n}^2 + 64.11186 \text{ S}_{w}^2 \text{ n}^3 - 0.16758 \text{ S}_{w}^3$$

$$- 3.70289 \text{ S}_{w}^3 \text{ n} + 130.8107 \text{ S}_{w}^3 \text{ n}^2 + 111.3276 \text{ S}_{w}^3 \text{ n}^3$$
 (B9)

(B3)

curves in figure 8 of reference 4. The small double-valued portions of the curves on the CDTH is used for the storage of these coefficients. This is a representation of the figure are not reflected in equation (B9).

momentum parameter as a function of correlation number and wall temperature function, (7) In addition to these curve fits, LAMNAR uses another curve fit indirectly Z

$$N = 0.04631 + 5.43220 \text{ n} + 4.51903 \text{ n}^2 + 19.01831 \text{ n}^3 - 0.00367 \text{ S}_w + 2.25400 \text{ S}_w \text{n}$$

$$- 10.49775 \text{ S}_w \text{n}^2 + 62.76597 \text{ S}_w \text{n}^3 + 0.00481 \text{ S}_w^2 - 0.06672 \text{ S}_w^2 \text{ n}$$

$$- 12.71732 \text{ S}_w^2 \text{n}^2 + 115.00986 \text{ S}_w^2 \text{n}^3 + 0.00651 \text{ S}_w^3 - 0.20637 \text{ S}_w^3 \text{ n}$$

$$- 2.95270 \text{ S}_w^3 \text{n}^2 + 62.53113 \text{ S}_w^3 \text{n}^3$$
 (B10)

eq. (1)) of this report) for a given S_{W} is assumed to be represented by the following The momentum parameter (see This is a representation of figure 4 of reference 4. linear function:

are calculated near statement 100 in LAMNAR. In these calculations, the terms in equation (B10) are used. and B The coefficients A

APPENDIX C

CHANGES TO PROGRAM FOR A GAS OTHER THAN AIR

BLAYER is easily altered so that it applies for gases other than air. The necessary changes are all made in the PRECAL subroutine. These changes are the following:

(1) At the beginning of PRECAL, new curve-fit coefficients must be read in by DATA statements for the CMU, CPR, and CTC arrays. These are the coefficients of the following curve fits (see appendix B):

$$\frac{\mu}{\mu_{Sl}} = f\left(\frac{T}{T_{Sl}}\right)$$

$$Pr = f\left(\frac{T}{T_{Sl}}\right)$$

$$\frac{k}{k_{Sl}} = f\left(\frac{T}{T_{Sl}}\right)$$

in the DATA statements and later in PRECAL in the calls on CURVFT where CMU, CPR, If the number of coefficients changes from five in any case, this must be reflected both and CTC are used.

- values are stored at the beginning of PRECAL after the DATA statements for CMU, CPR, These (MUSLE, MUSLM), and thermal conductivity (TCSLE, TCSLM) must be changed. (2) The sea-level reference values of temperature (TSLE, TSLM), viscosity and CTC.
- (3) Near statement 10 in PRECAL, the two statements storing values into TCON should be removed. The computation of TR1 using TSLM would then become state-
- (4) Shortly after statement 210 in PRECAL, the computation of SUTHL(I) should be changed. A temperature-viscosity law of the following form is used in the program.

$$\frac{\mu}{\mu_0} = k_{\rm Su} \frac{T}{T_0} \tag{C1}$$

with the constant k_{Su} having the famous Sutherland value for air

$$k_{SU} = \left(\frac{T}{T_0}\right)^{1/2} \frac{T_0 + S}{T + S}$$
 (C2)

where $\mathscr S$ is Sutherland's constant (TCON). SUTHL(I) is the $k_{\mathbf S \mathbf U}$ of formulas (C1) and (C2). A temperature-viscosity law agreeing with formula (C1) must be used in the program, but the computation of k_{su} would have to change for a gas other than air.

A P P E N D I X D

SYMBOLS

constants in eqs. (2) to (4) and (14)

speed of sound, ft/sec; m/sec

local skin friction coefficient $_{
m f}$ specific heat at constant pressure, $(\mathrm{ft})(\mathrm{lbf})/(\mathrm{slug})(^{\mathrm{O}}\mathrm{R});\ \mathrm{J/(kg)(K)}$

function of transformed momentum thickness, eq. (7)

form factor, $\delta */\theta$

transformed form factor for adiabatic flow, also called incompressible form factor,

$$\int_0^{\delta_{\rm tr}} \left[1 - \left(\frac{{\rm U}}{{\rm U}_{\rm e}} \right) \right] {\rm d}^{\rm Y}_{\rm tr} / \theta_{\rm tr}$$

transformed form factor for nonadiabatic flow, $\,\delta_{
m tr}^*/\, heta_{
m tr}$

enthalpy, (ft)(lbf)/slug; J/kg

shape factor based on momentum thickness, $(\theta^2/
u_{
m w})$ (due/dx)

mean shape factor based on momentum thickness, eq. (25)

coefficient of thermal conductivity, $(\mathrm{ft})(\mathrm{lbf})/(\mathrm{ft})(\mathrm{sec})(^0\mathrm{R});\ \mathrm{J/(m)(sec)(K)}$ K k su L

constant in Sutherland's viscosity-temperature relation, eqs. (C1) and (C2)

total distance along boundary-layer surface, ft; m

shear-stress parameter, eqs. (20) and (B7)

Mach number Z

 $'(T_{aw} - T_w)$ momentum parameter, eqs. (1) and (2) local Nusselt number, $x \left(\frac{\partial T}{\partial y} \right)_{w} / (T_{aw}$ Nux

correlation number (pressure gradient parameter), eqs. (4) and (14)

reciprocal of power in power law, eq. (36)

pressure, lbf/ft^2 ; N/m^2

Prandtl number, $\mu c_{\rm p}/k$

Pr

heat transfer per unit area, $(\mathrm{ft})(\mathrm{lbf})/(\mathrm{ft}^2)(\mathrm{sec});~\mathrm{J/(m}^2)(\mathrm{sec})$

Reynolds number at the wall based on surface length, $u_{\rm e} x/\nu_{\rm w}$

Reynolds number based on momentum thickness, u_e^{θ/ν_W}

universal gas constant, $(\mathrm{ft})(\mathrm{lbf})/(\mathrm{slug})(^{O}R);~J/(\mathrm{kg})(K)$

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enthalpy function, $(h'/h_0') - 1$

temperature, ⁰R; K

adiabatic or recovery wall temperature, ^OR; K

transformed longitudinal velocity, $(a_0'/a_e)u$, ft/sec; m/sec

longitudinal velocity parallel to boundary-layer surface in x-direction (see fig. 4), ft/sec; m/sec

coordinate for input of surface geometry (see figs. 4 and 5), ft; m

transformed x-coordinate along body surface, ft; m:

$$x_{tr} = \int_0^x \frac{P_e}{k_{Su}} \frac{\left(T_e}{P_0^2}\right)^{1/2} dx$$
 in laminar flow

$$X_{tr} = \sqrt{\frac{T_0'}{\overline{T}} \left(\frac{T_0}{T_0'}\right)^{2\gamma - 2}} dx \quad \text{in turbulent flow}$$

coordinate parallel to body surface in streamwise direction (see fig. 4),

×

coordinate for input of surface geometry (see figs. 4 and 5), ft; m transformed Y-coordinate normal to body surface, ft; m:

$$Y_{tr} = \left(\frac{T_e}{T_0^0}\right)^{1/2} \int_0^y \frac{\rho}{\rho_0^t} dy$$
 for both laminar and turbulent flow

coordinate normal to body surface (see fig. 4), ft; m

>

- ratio of specific heats
- boundary-layer thickness, ft; m

Ø

- transformed boundary-layer thickness, ft; m $\delta_{\rm tr}$
- dy, ft; m nσ displacement thickness, *0
- $\left(\frac{U}{U} + S\right) dY_{tr}, ft; m$ transformed displacement thickness, $\delta_{
 m tr}^*$
- normalized distance from wall, y/δ u
- $1 \frac{u}{d}$ dy, ft; m momentum thickness,
- $(1 \frac{U}{U_e}) dx_{tr}$, ft; m transformed momentum thickness, $heta_{
 m tr}$ θ
- Pohlhausen shape factor based on boundary-layer thickness, $(\delta^2/
 u_{
 m e})({
 m du_e}/{
 m dx})$
 - dynamic viscosity, (lbf)(sec)/ft 2 ; (N)(sec)/m 2 ュ
 - kinematic viscosity, μ/ρ , ft²/sec; m²/sec
 - density, $slug/ft^3$; kg/m^3 Q
- shear stress, lbf/ft^2 ; N/m^2

Subscripts:

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- critical \mathbf{cr}
- value external to boundary layer
- incompressible quantity
- instability inst
- sea-level value 28
- stagnation point value ₫**s**
- transformed quantity tr
- transition tran

- w wall or surface value
- local value based on x
- increment or difference in some quantity

0

- free-stream value; condition external to boundary layer, usually near
 - x = 0 (see fig. 6)
- 1, 2, 3, ... at station 1, 2, 3,

Superscripts:

total or stagnation condition, or quantity based on total or stagnation condition

evaluated at reference conditions (see ref. 19)

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